

# A Model-Based Approach Towards Identifying the Brain's Learning Algorithms

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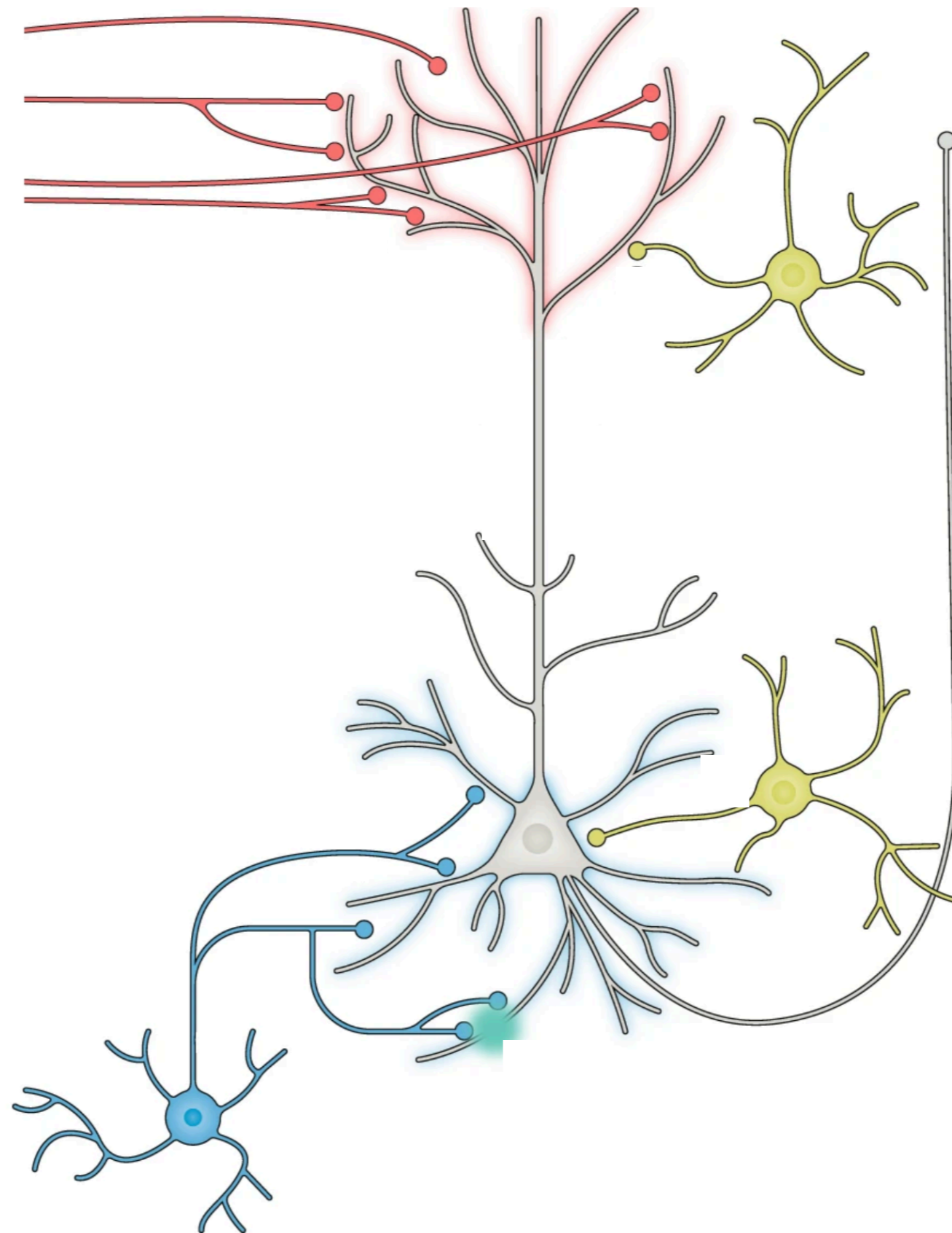
**MBCT Seminar**

*2021.01.25*

**Aran Nayebi**

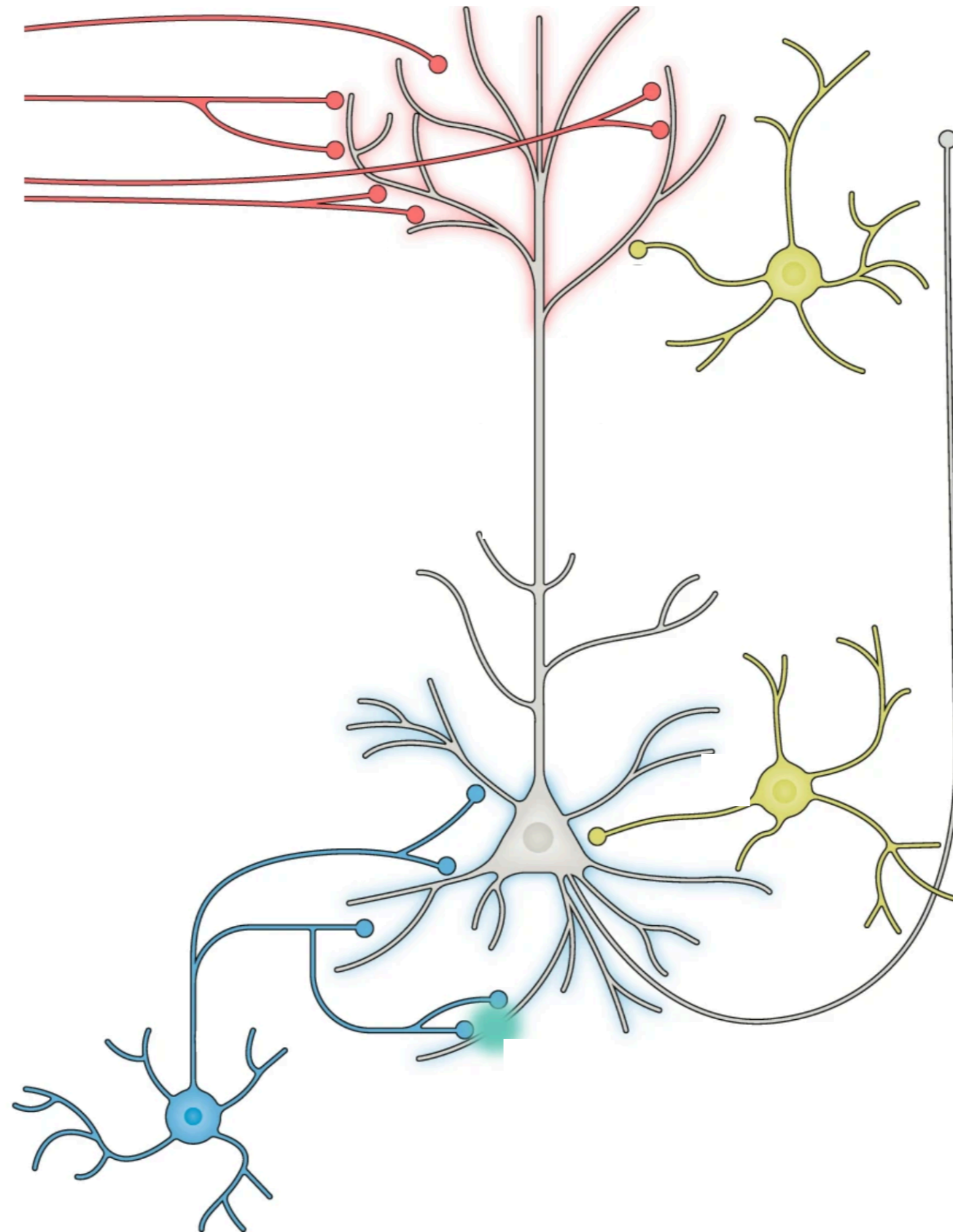
Neurosciences PhD Candidate  
Stanford University

# Problem set-up



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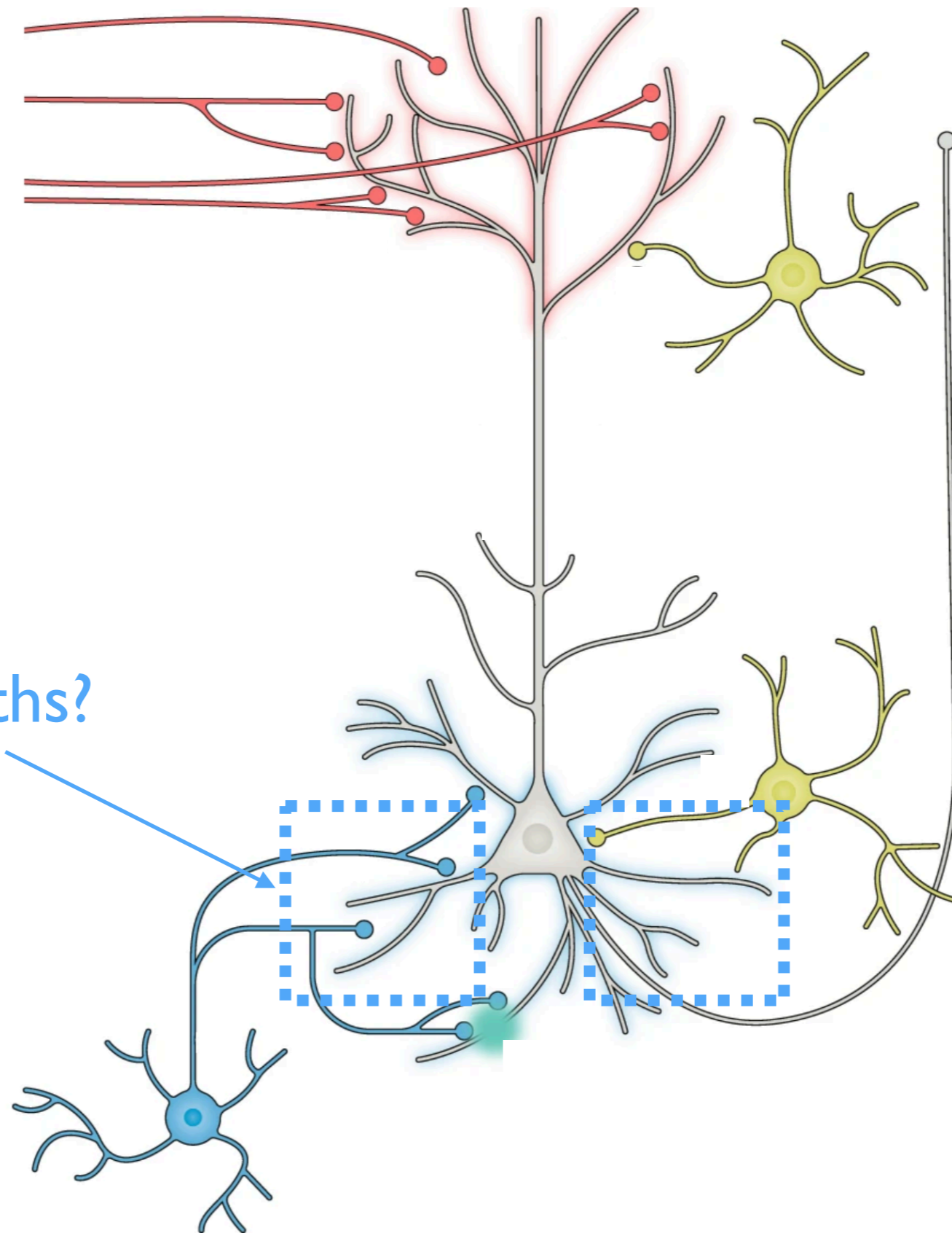
Post-synaptic activities?



# Problem set-up

Post-synaptic activities?

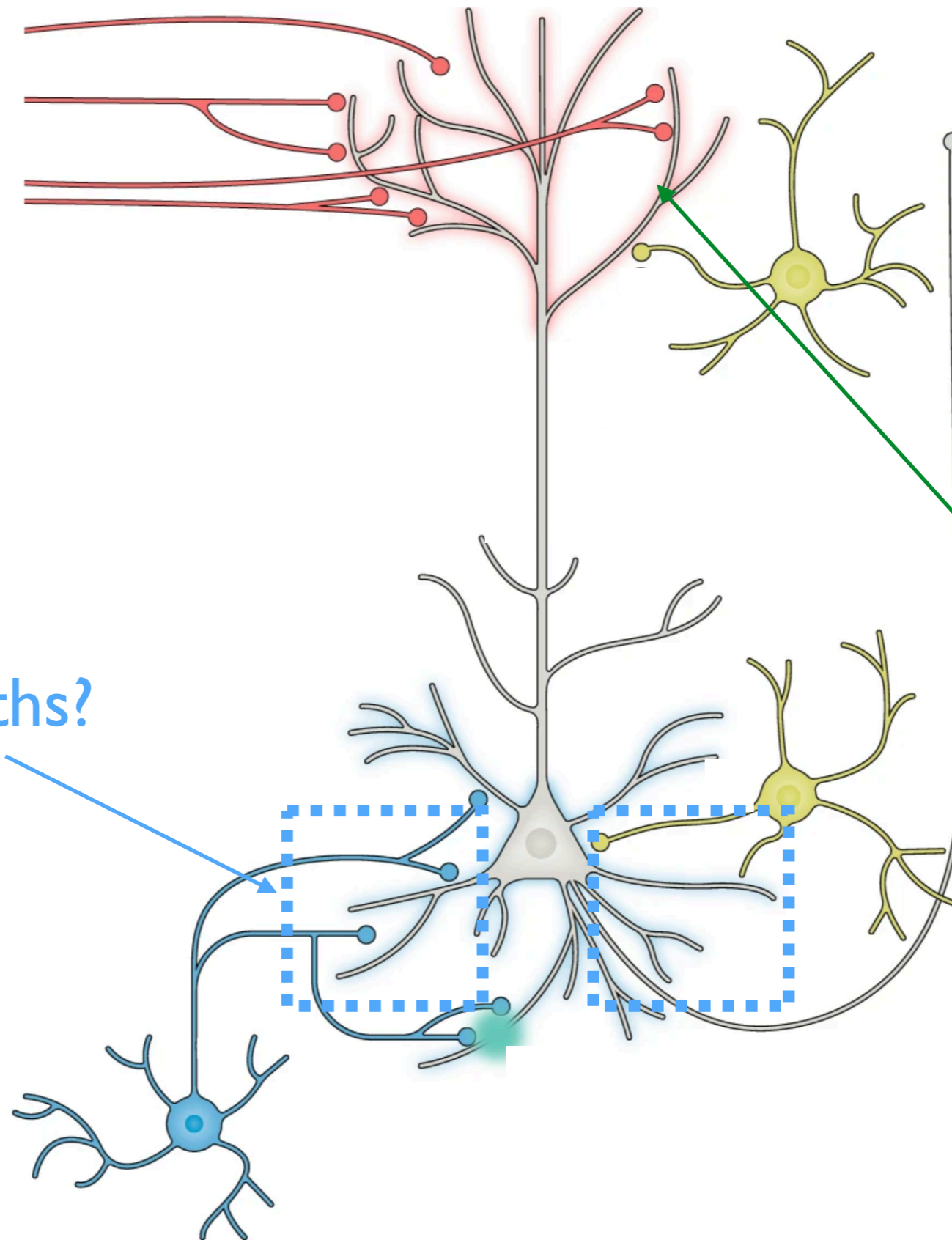
Synaptic strengths?



# Problem set-up

Post-synaptic activities?

Synaptic strengths?



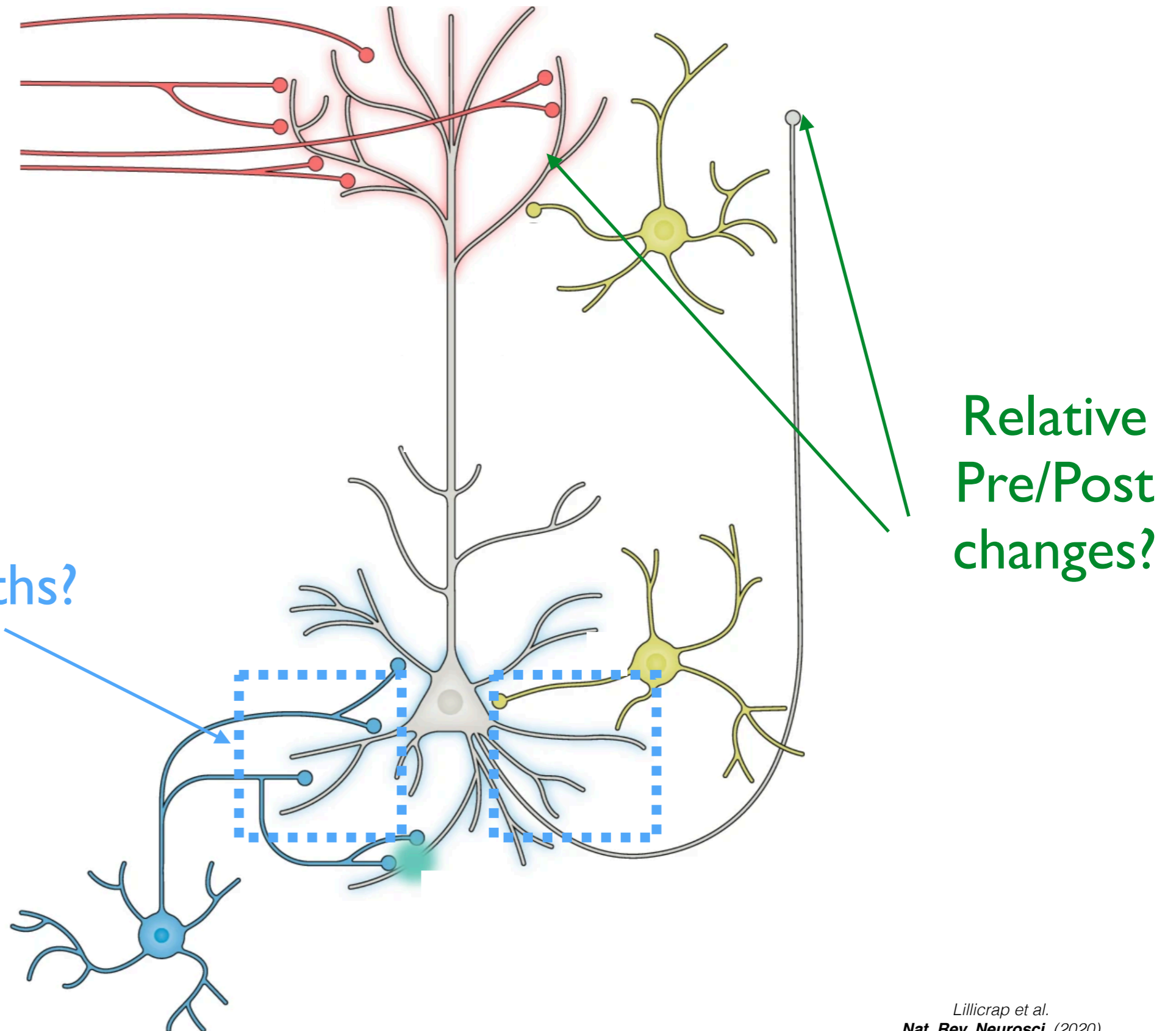
Relative Pre/Post changes?

# Problem set-up

Post-synaptic activities?

Cortical area?

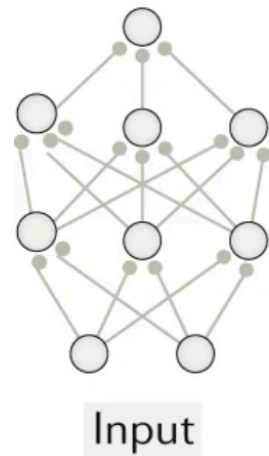
Synaptic strengths?



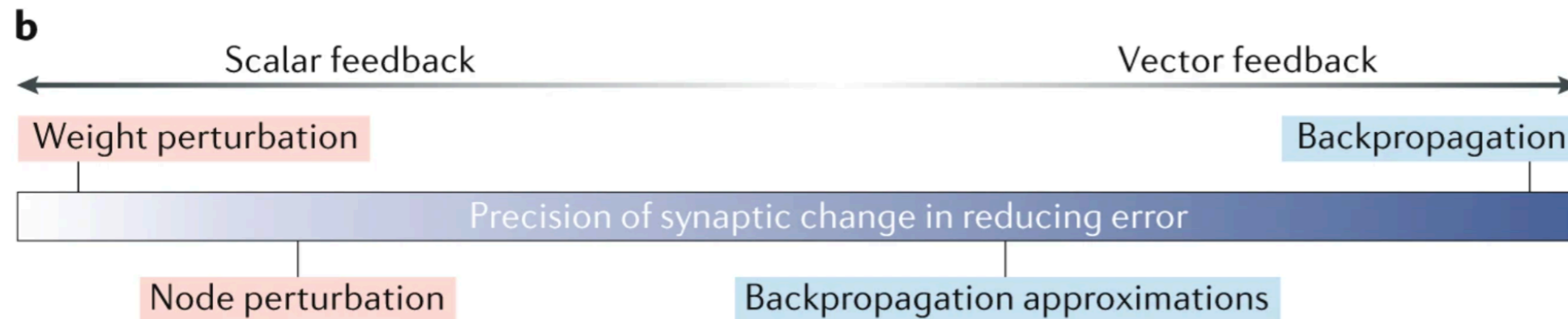
**Why might this problem be worth considering?**

# Spectrum of learning strategies

Feedforward network  
Output

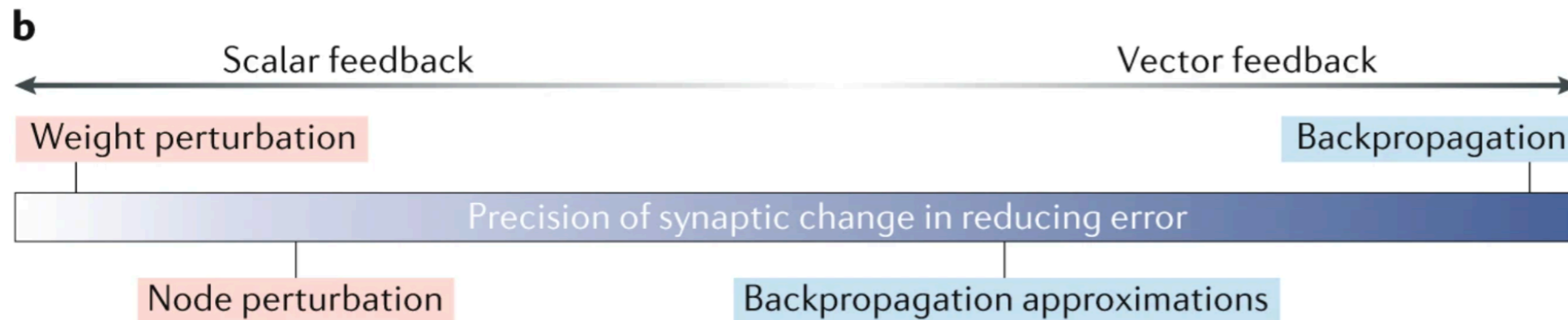


- Synapse undergoing learning
- Feedback signal (e.g. gradient)
- Feedback neuron (required for learning)
- Feedforward neuron (required for learning)
- Diffuse scalar reinforcement signal

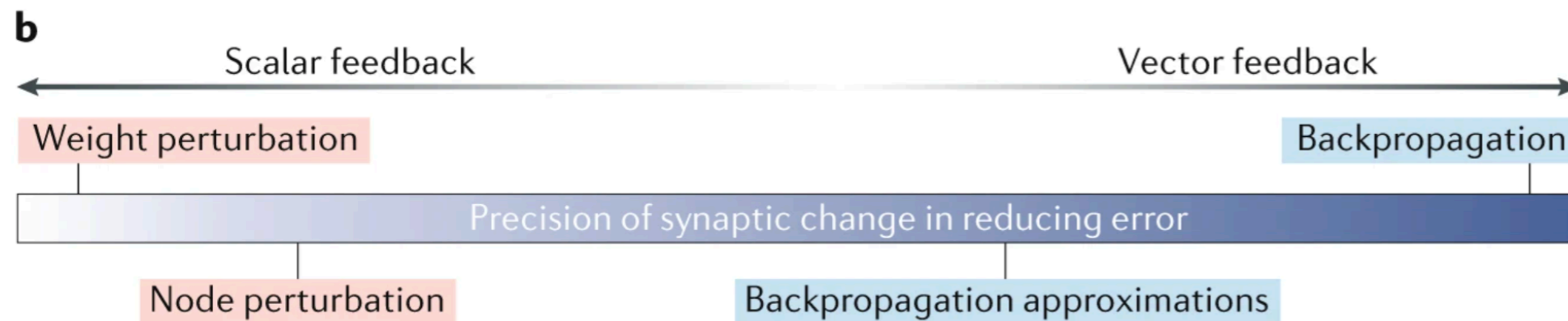
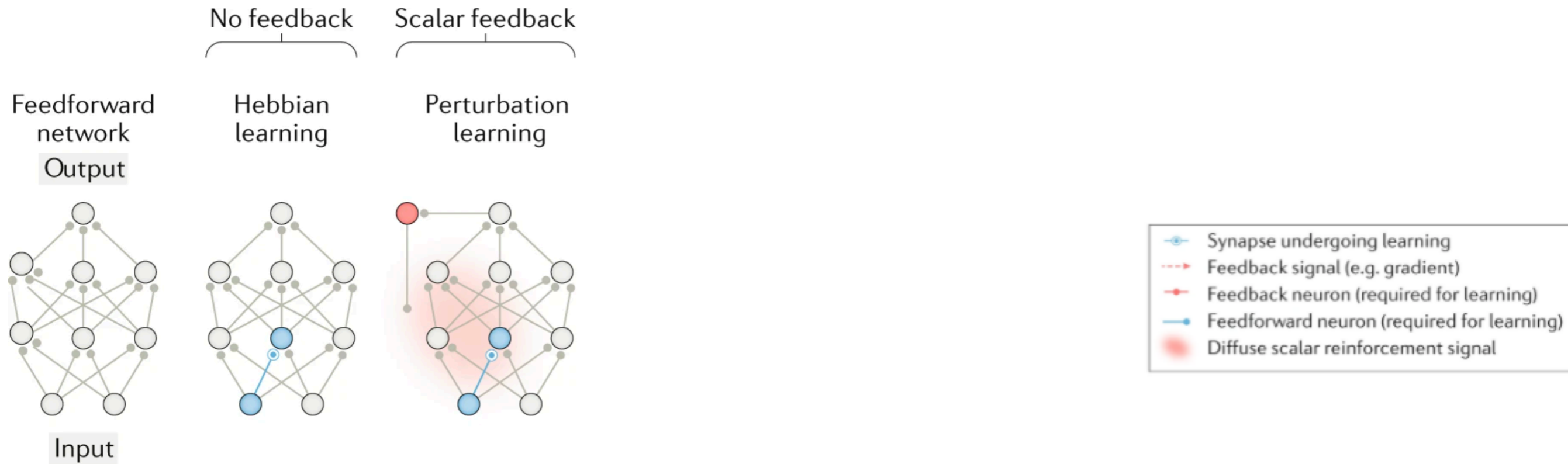




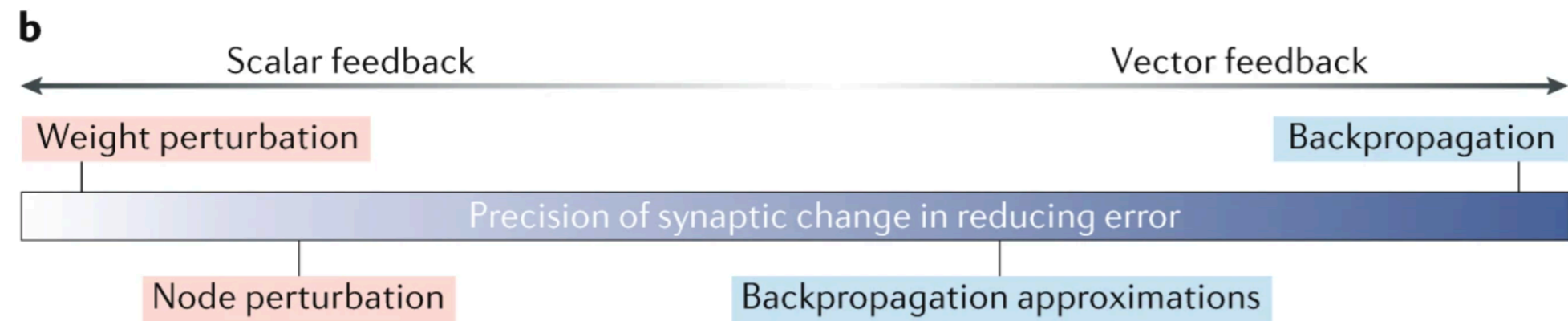
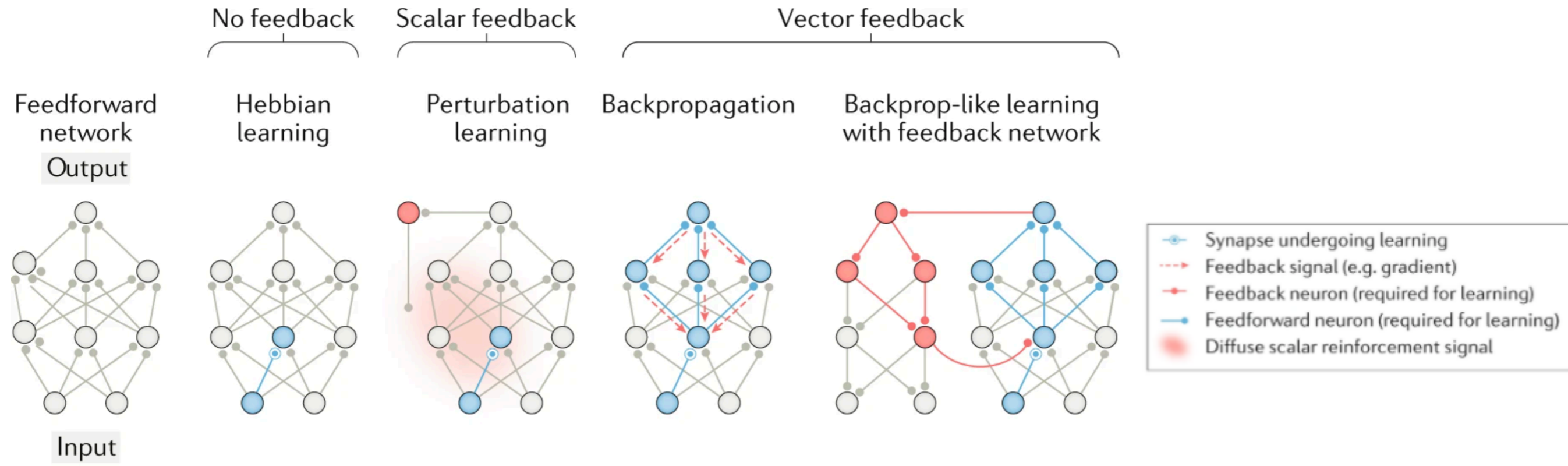
# Spectrum of learning strategies



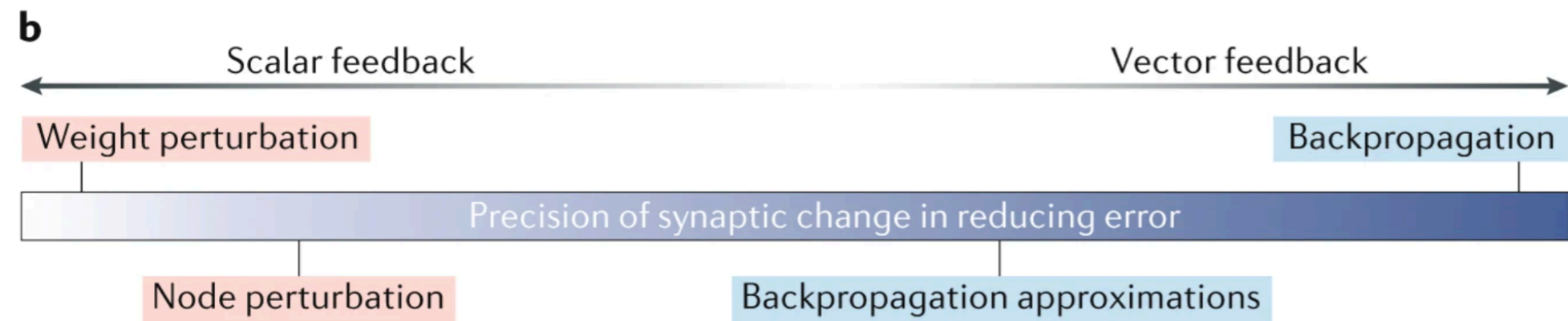
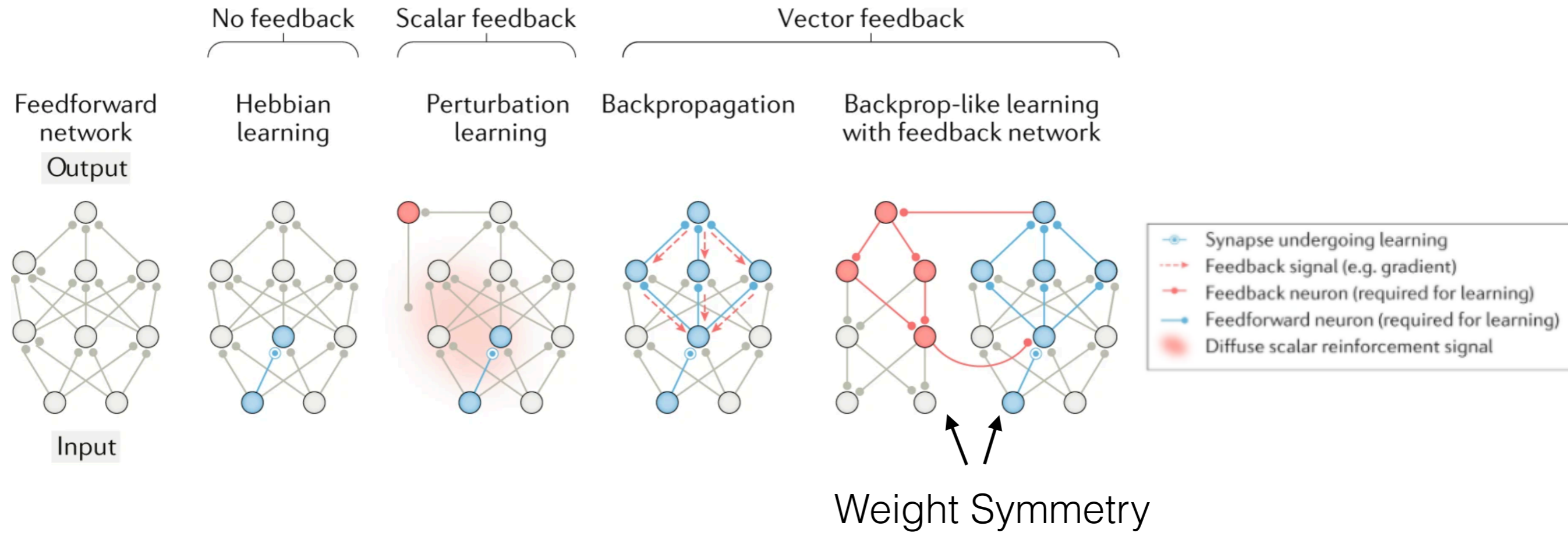
# Spectrum of learning strategies



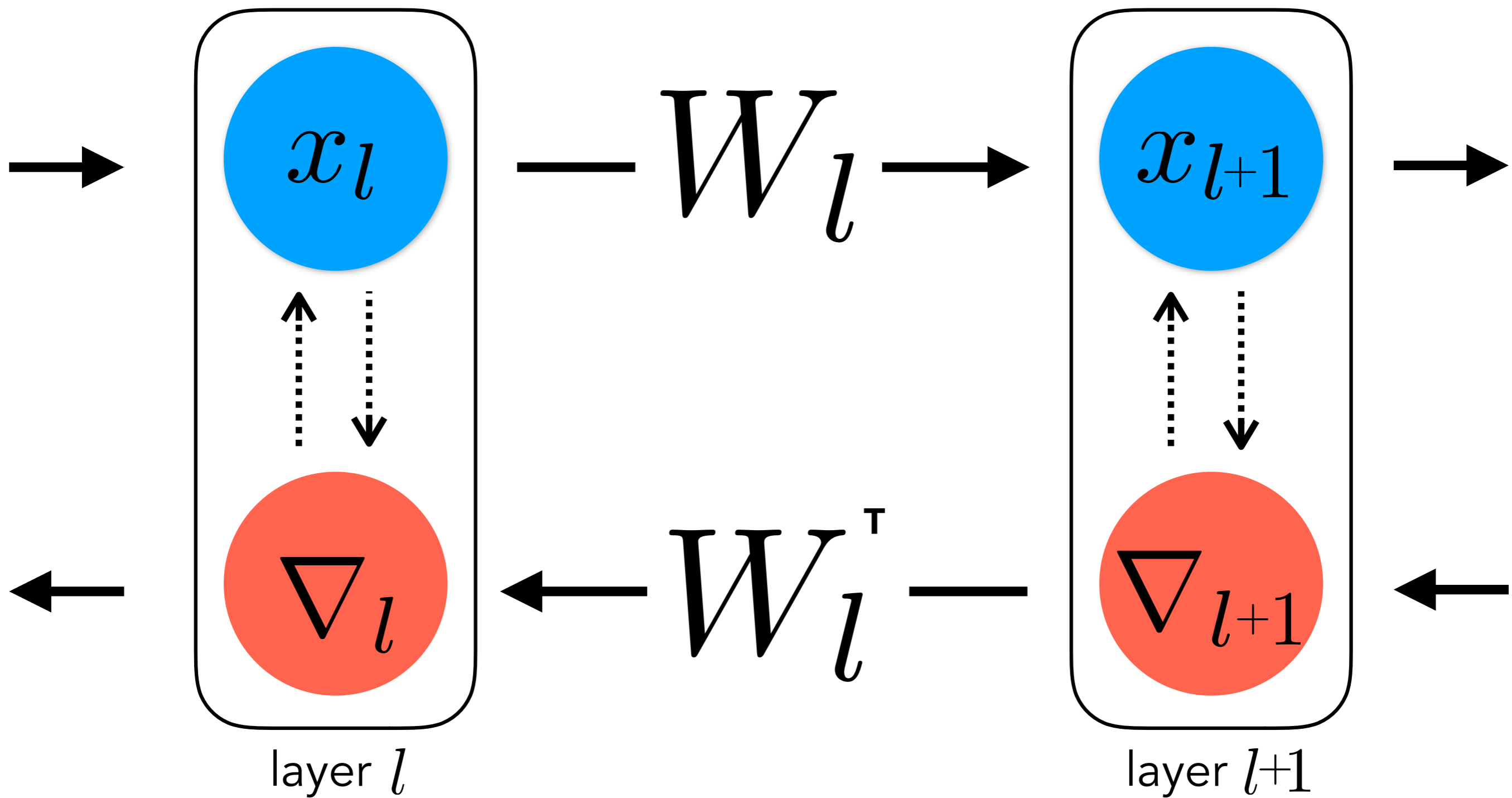
# Spectrum of learning strategies



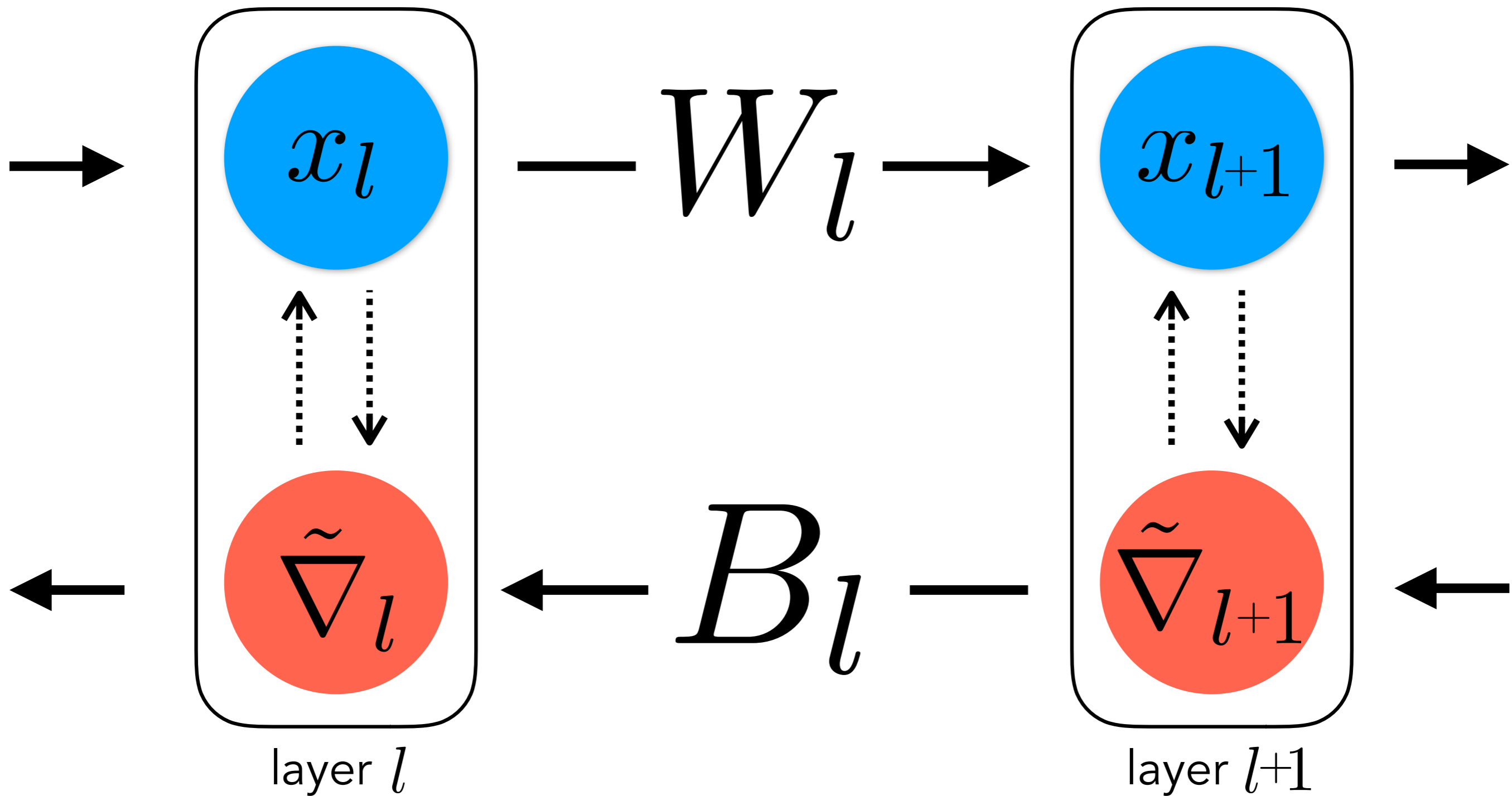
# Spectrum of learning strategies



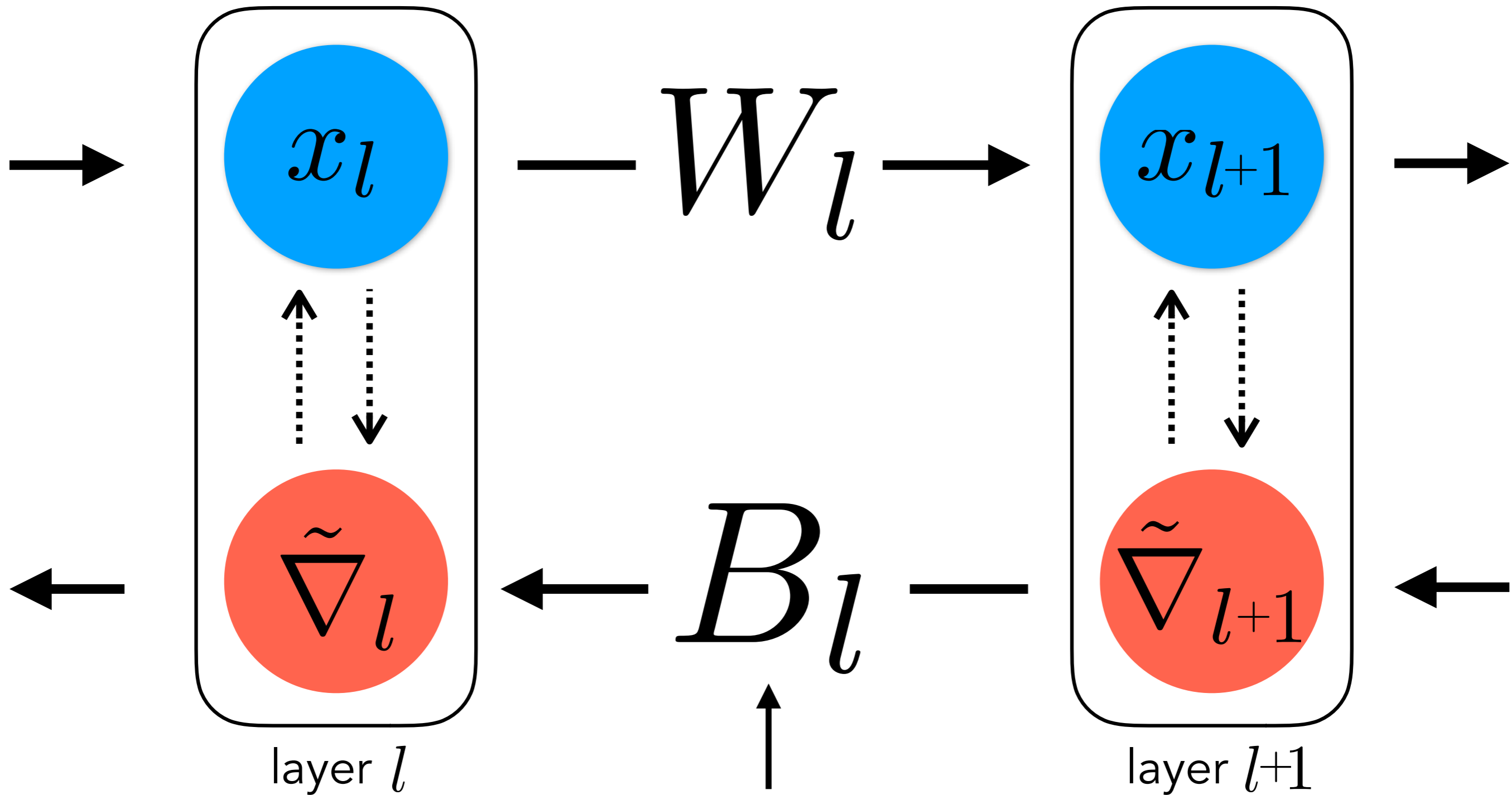
# Relaxing the weight symmetry requirement



# Relaxing the weight symmetry requirement



# Feedback Alignment (FA)



**Feedback Alignment (FA):**  $B$  is random

# Comparing Feedback Alignment to Backprop

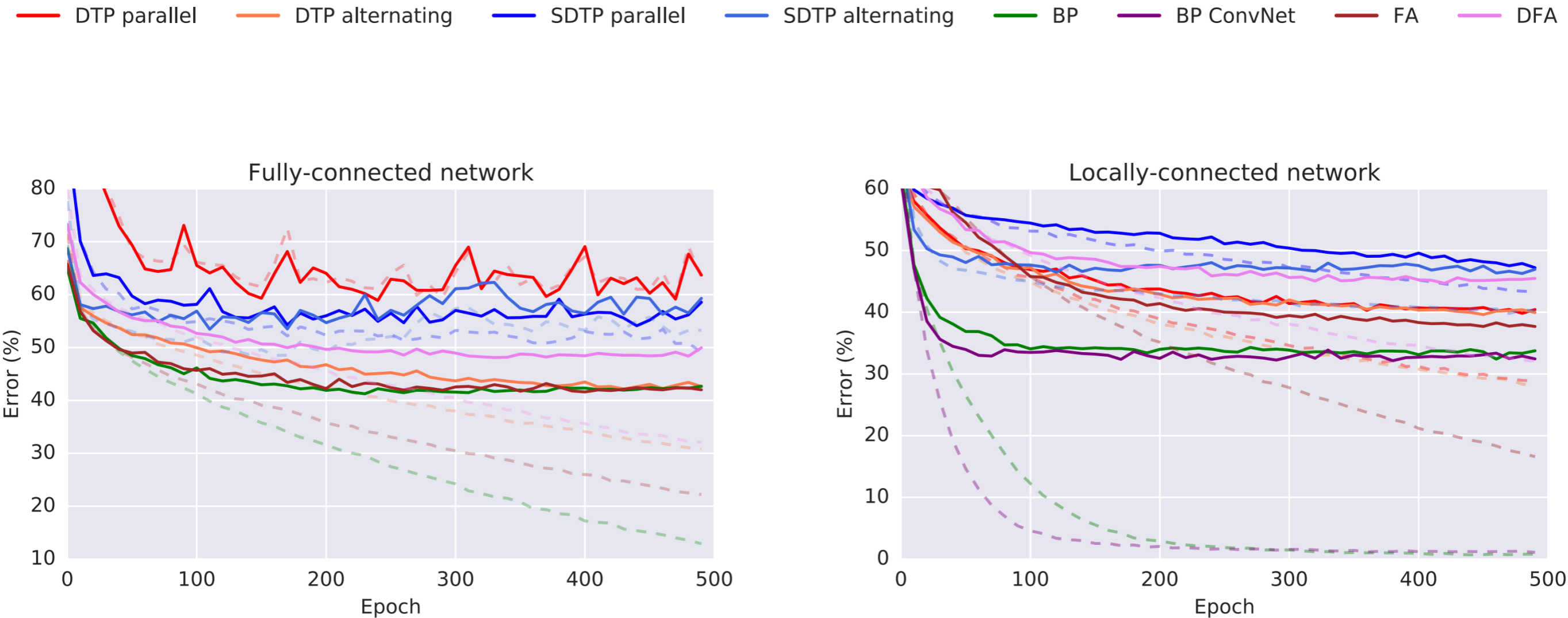


Figure 2: Train (dashed) and test (solid) classification errors on CIFAR.



# Scales as Backprop does on simple tasks

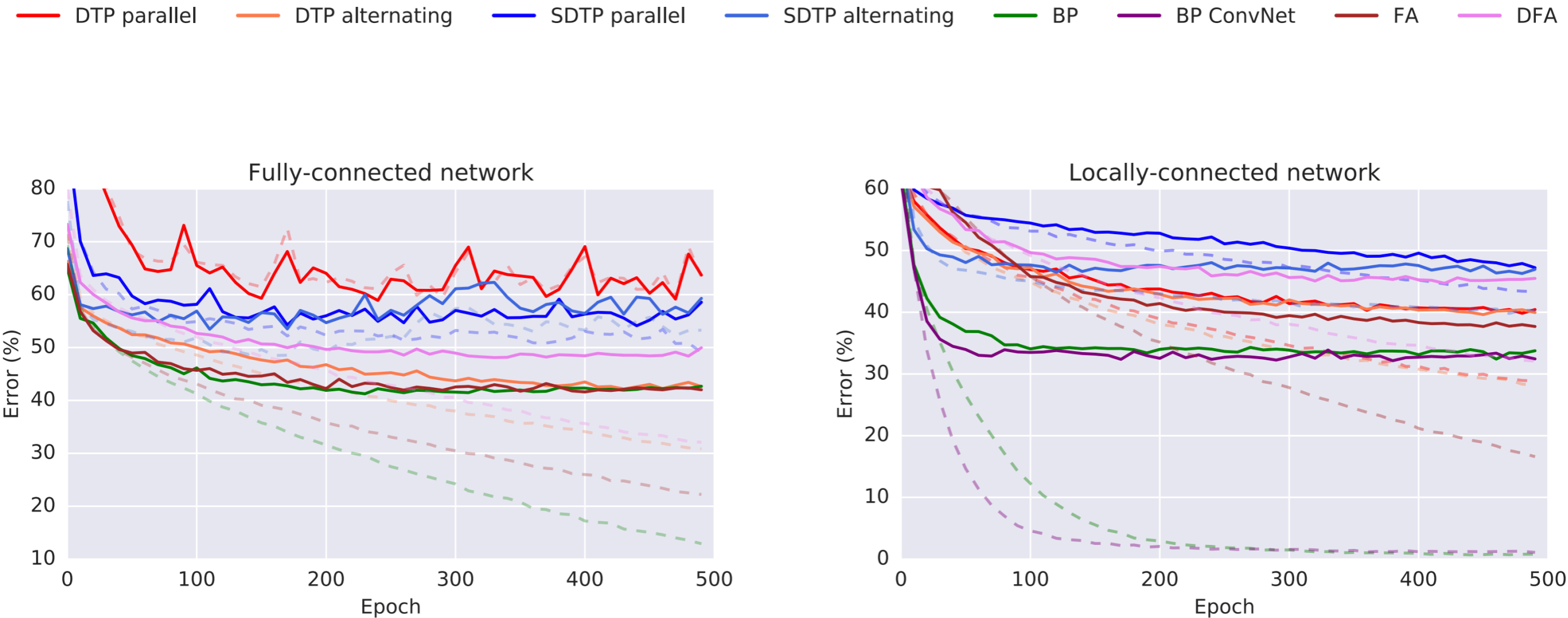


Figure 2: Train (dashed) and test (solid) classification errors on CIFAR.

Similar performance between FA and Backprop on small tasks.

# Does *not* scale as Backprop does on harder tasks

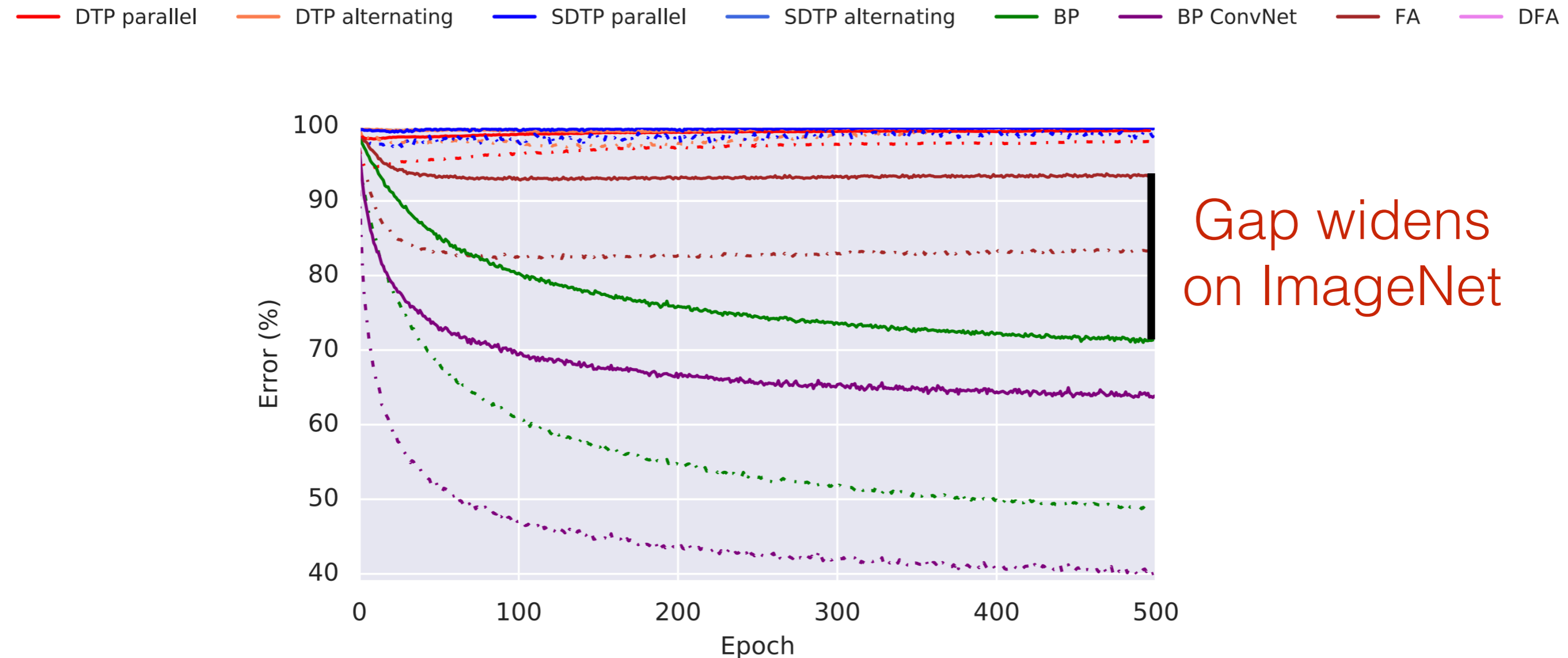
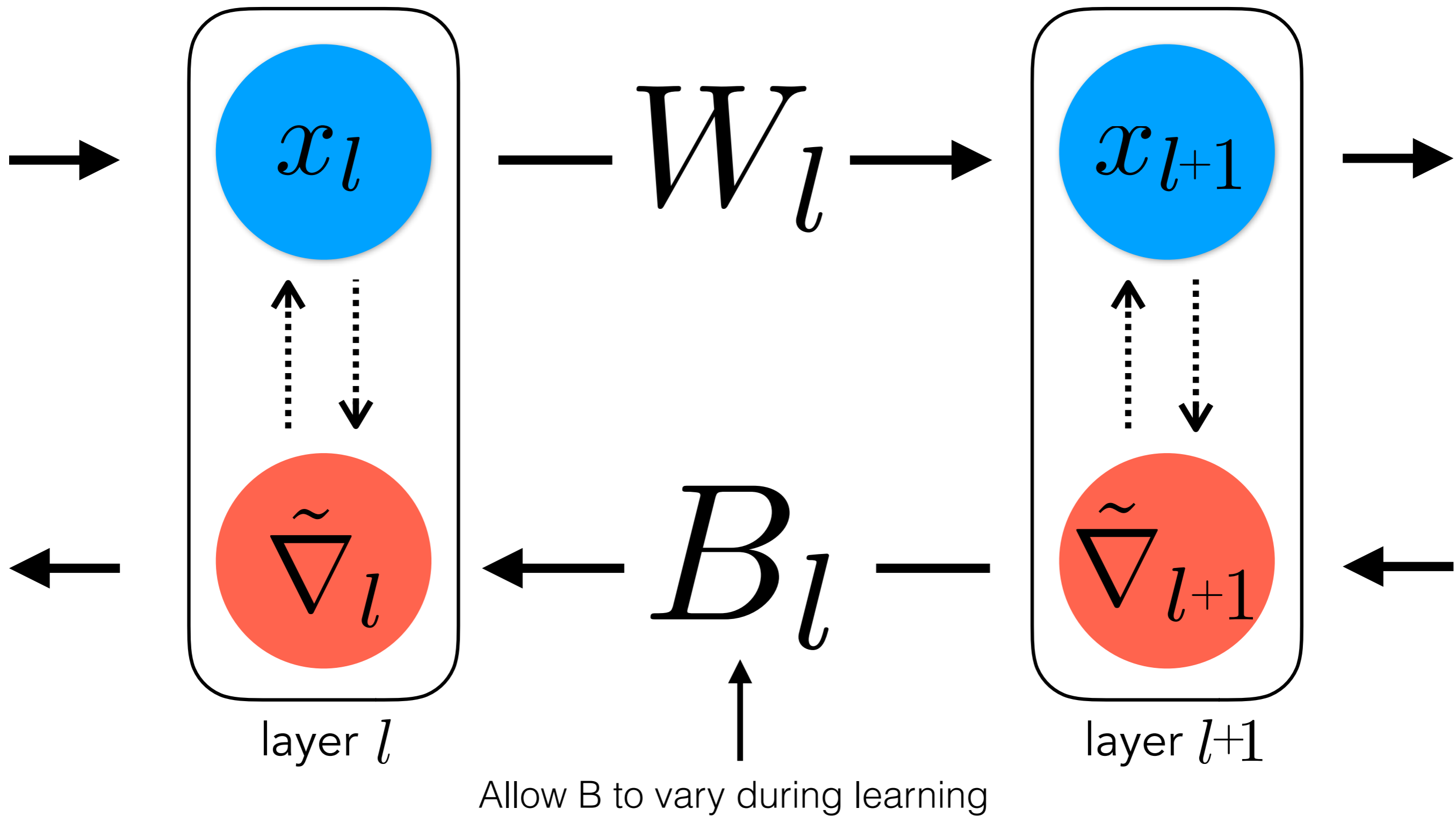
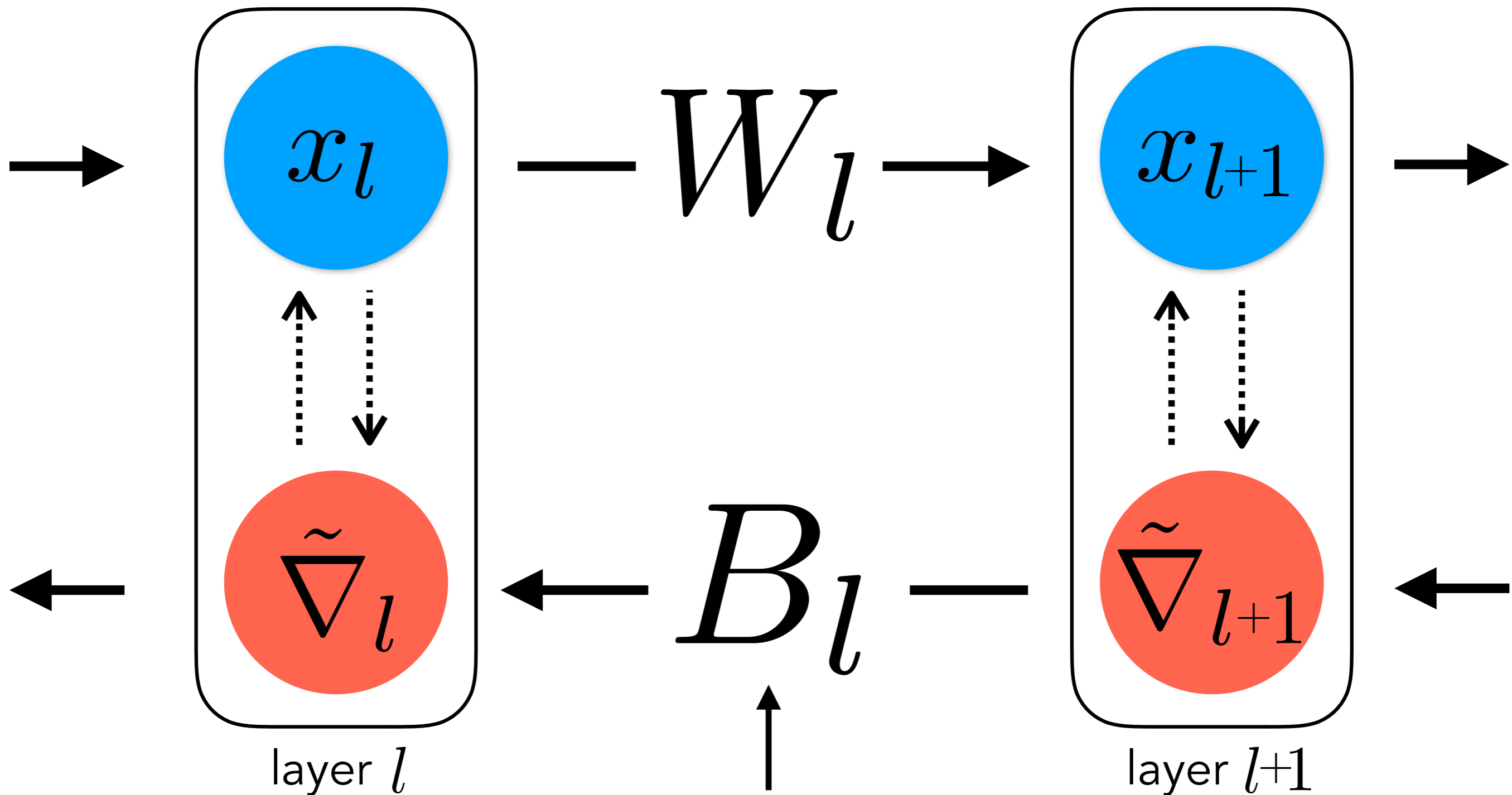


Figure 3: Top-1 (solid) and Top-5 (dotted) test errors on ImageNet. Color legend is the same as for figure 2.

# Imposing dynamics on the backward weights



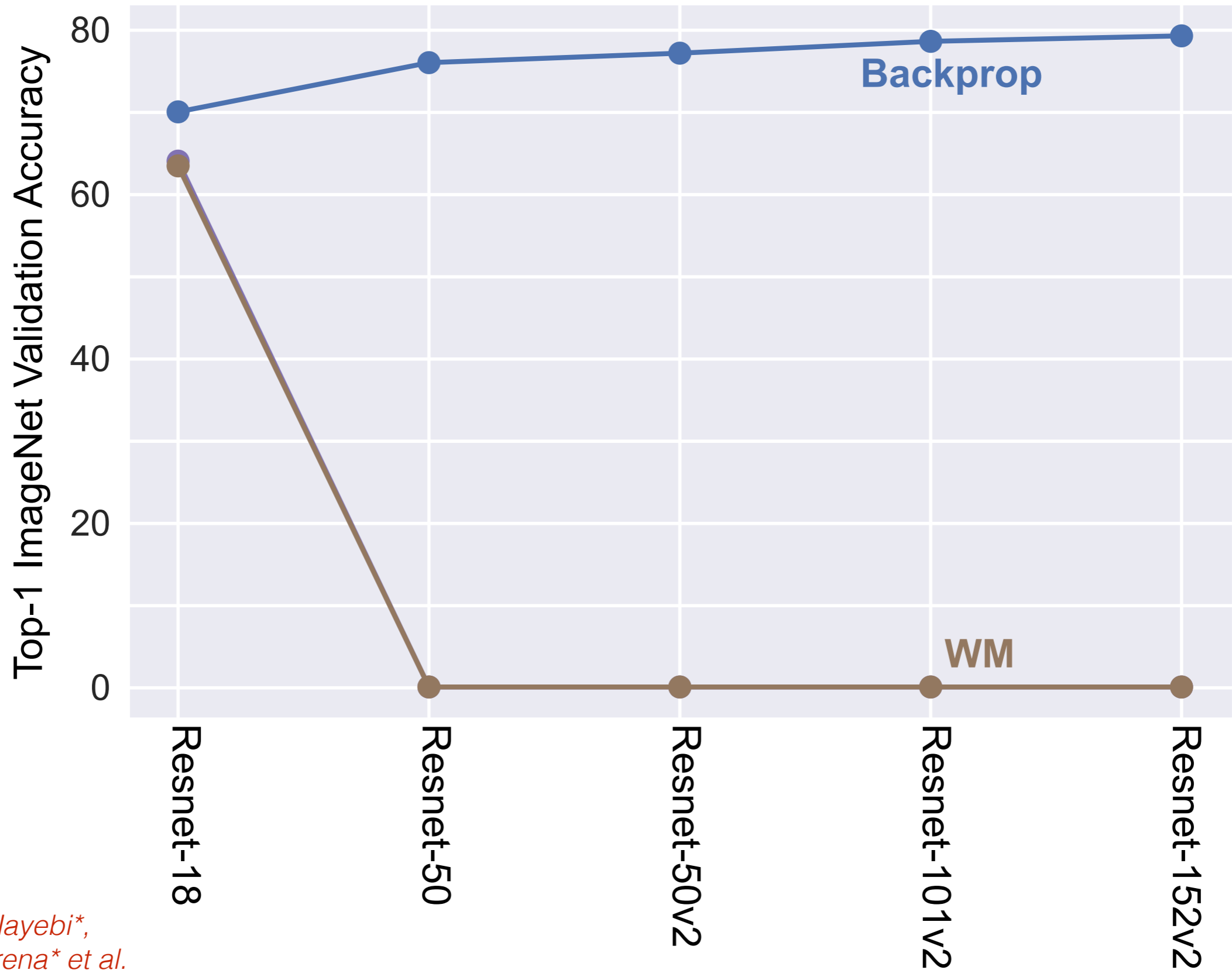
# Weight Mirror (WMM)



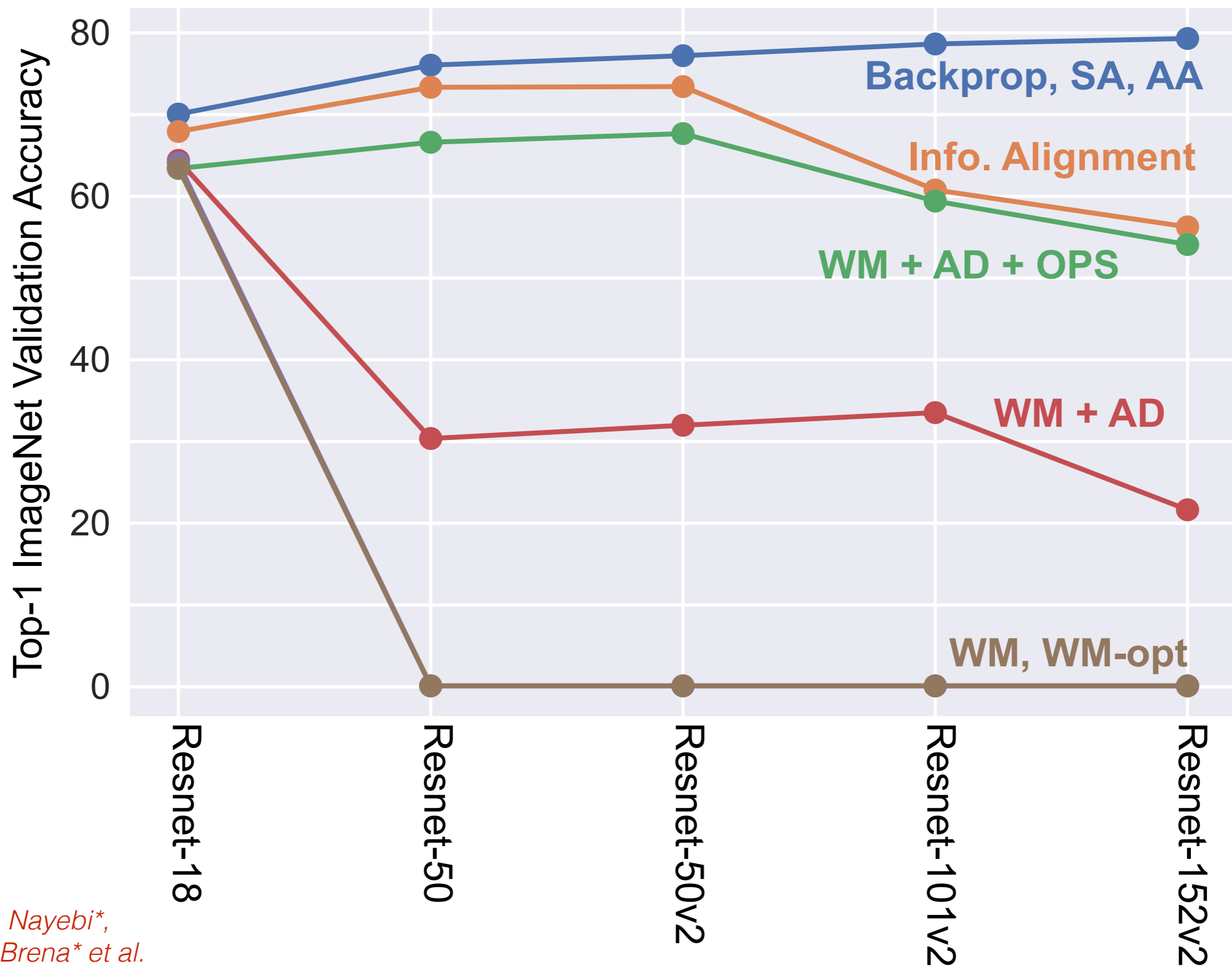
**Weight Mirror (WM):**  $B$  gradually aligns with  $W$

~~**Feedback Alignment (FA):**  $B$  is random~~

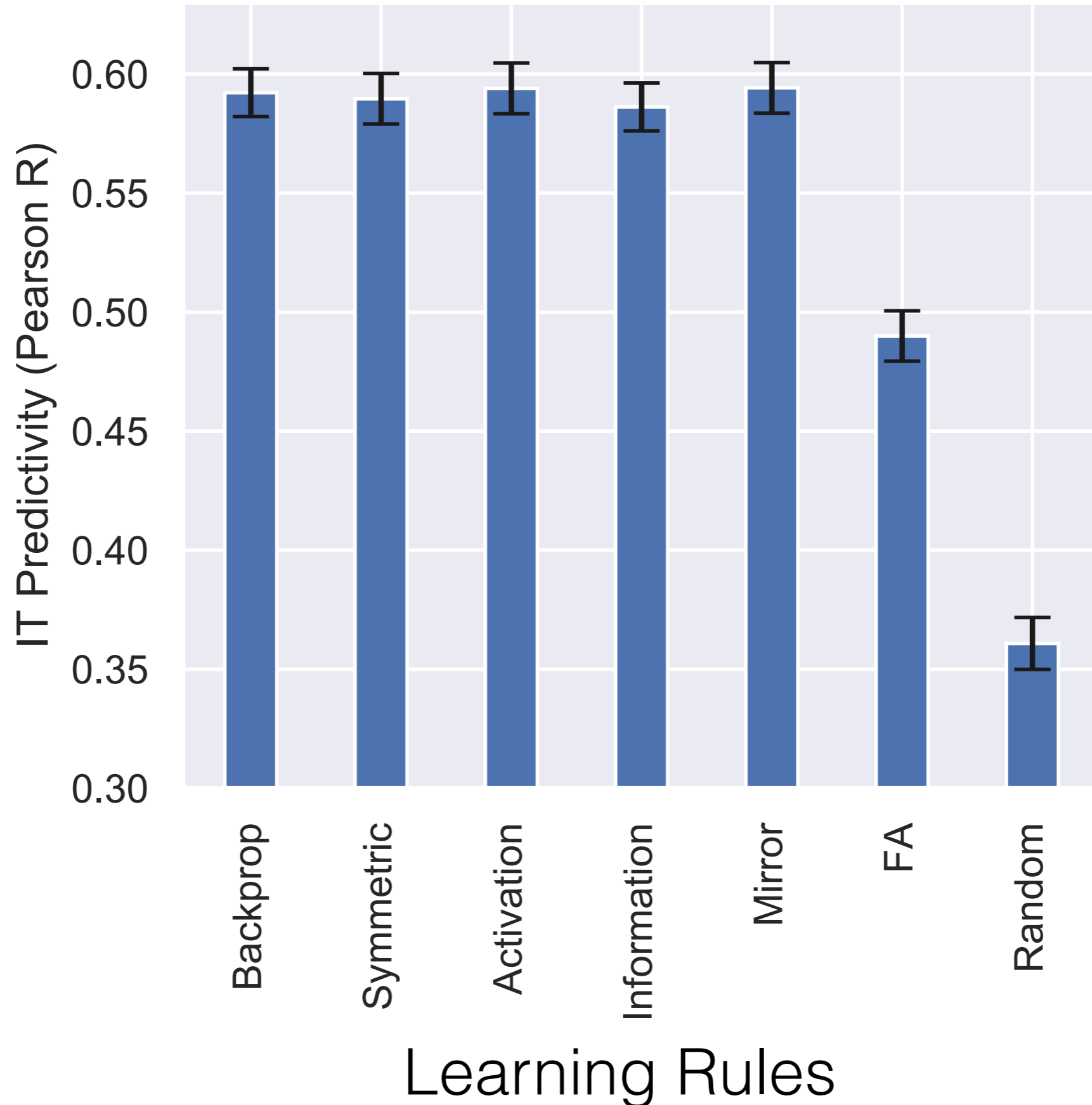
# Weight Mirror does not transfer across architectures



# Searching alternatives to Backprop scales across architectures



# Current neural data is insufficient to separate these alternatives



Can fit single learning rule to post-synaptic activities alone




# Can fit single learning rule to post-synaptic activities alone

nature  
neuroscience

Article | Published: 02 November 2015

## **Inferring learning rules from distributions of firing rates in cortical neurons**

Sukbin Lim, Jillian L McKee, Luke Woloszyn, Yali Amit, David J Freedman, David L Sheinberg & Nicolas Brunel 

# Can fit single learning rule to post-synaptic activities alone

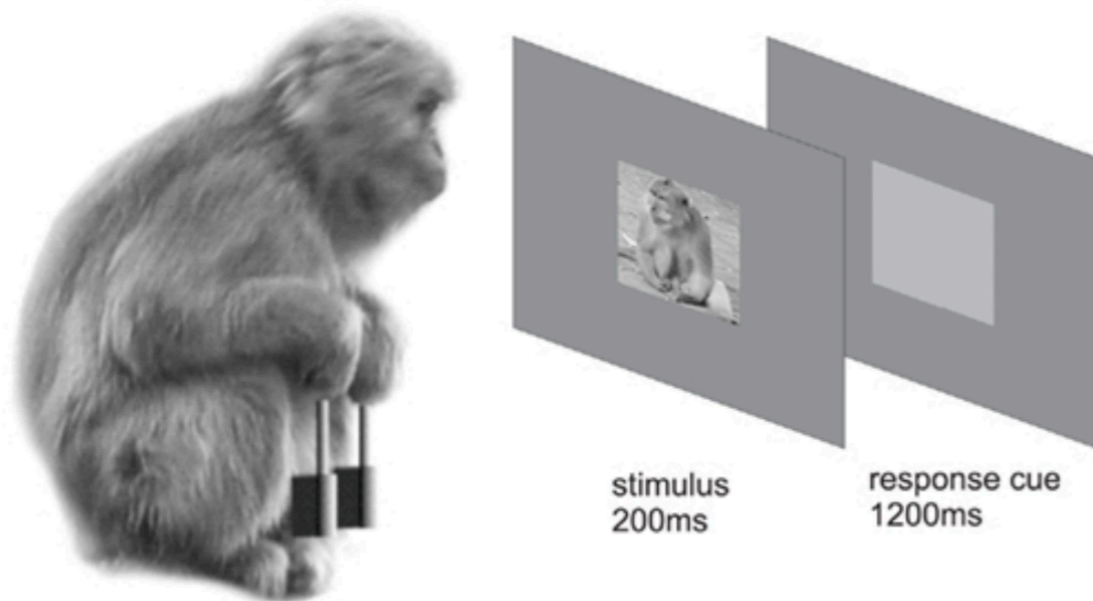
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## Inferring learning rules from distributions of firing rates in cortical neurons

Sukbin Lim, Jillian L McKee, Luke Woloszyn, Yali Amit, David J Freedman, David L Sheinberg & Nicolas Brunel [✉](#)

- ▶ Each session uses 125 novel & 125 familiar stimuli; macaque IT




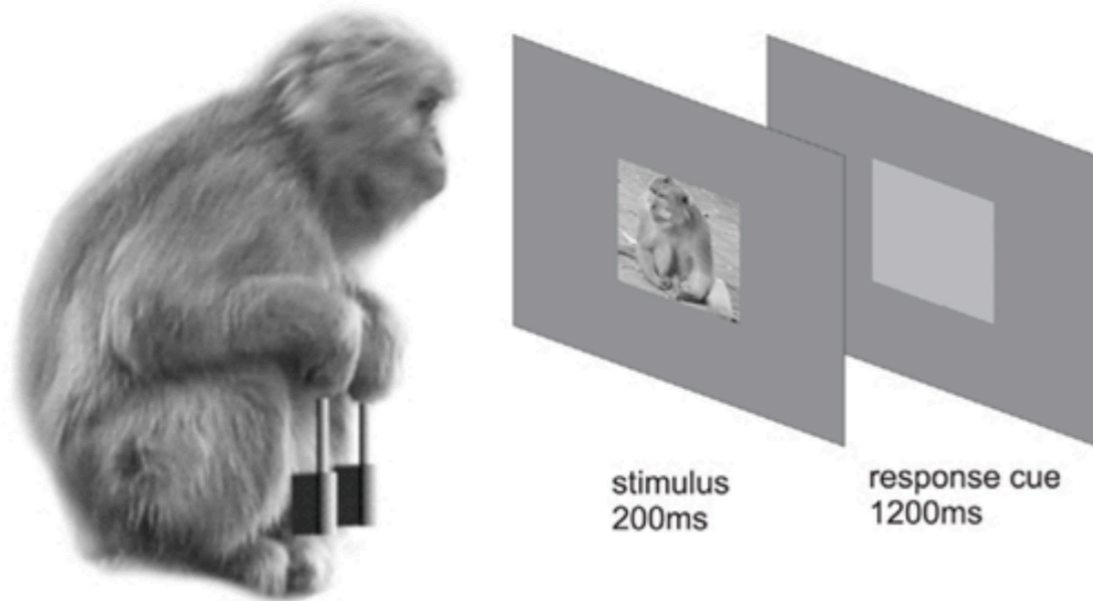
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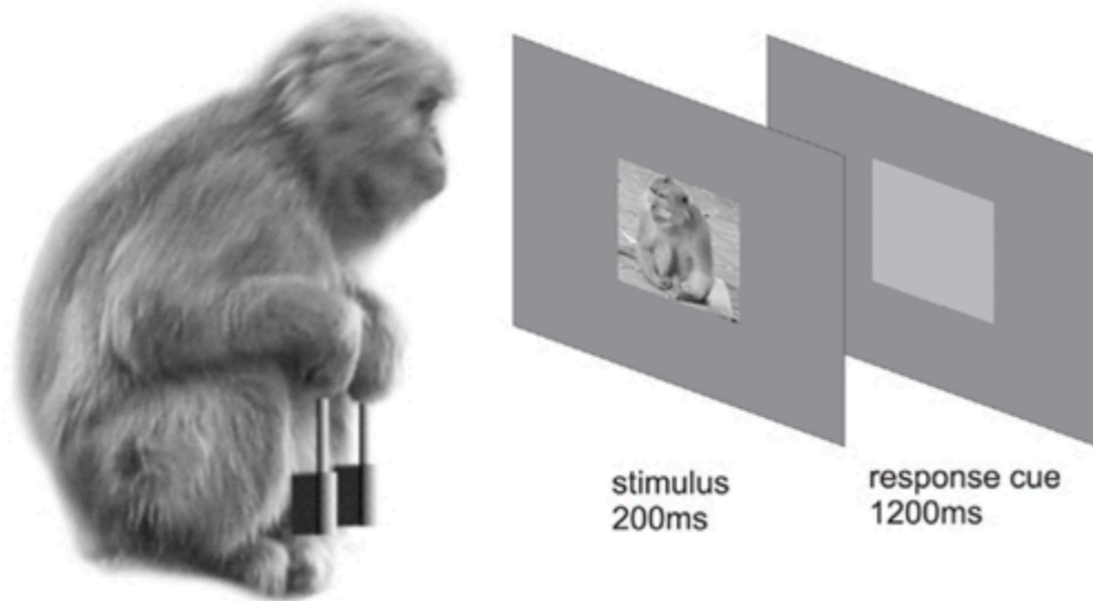
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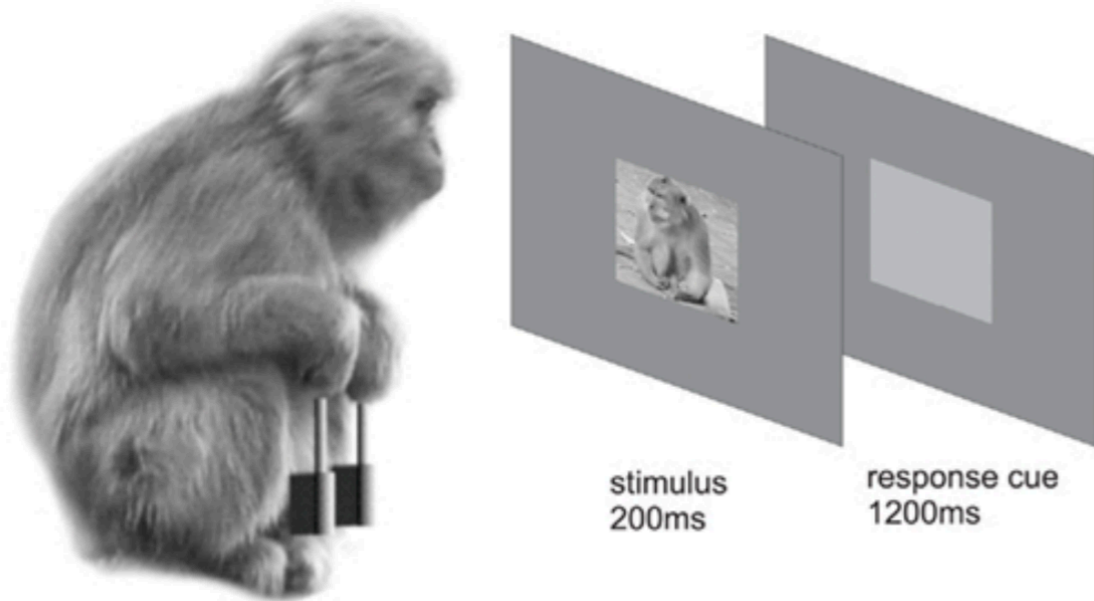
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Fits a *single* learning rule class (Hebbian) to data

# “Virtual Experimental” Approach

What would you need to measure  
to reliably distinguish *classes* of learning rules?

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to reliably distinguish *classes* of learning rules?

With artificial neural networks, we can measure anything we want & know the ground truth learning rule we trained the model with

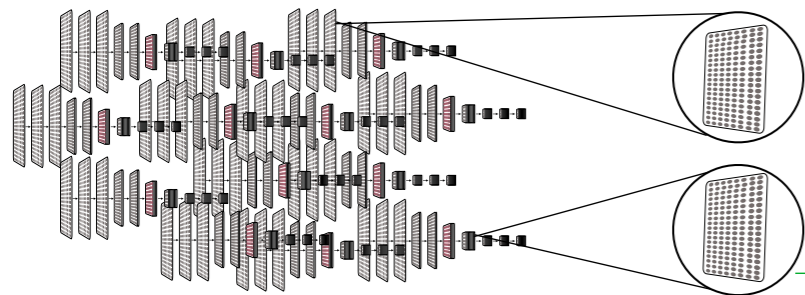
What would you need to measure to reliably distinguish *classes* of learning rules?

**Hypothesis:** measuring post-synaptic activities from a neural circuit on the order of several hundred units, may provide a good basis on which to identify learning rules.



# “Virtual Experimental” Approach

## Data Generation



10 architectures, 4 tasks, 12  
hyperparameter settings, 4  
learning rules

# Generating a large-scale dataset

Learning Rules	Tasks	Architectures	Hyperparameters
SGD+Momentum (SGDM)	ImageNet (supervised)	ResNet-34v2	Batch size (128, 256, 512)
Adam	SimCLR (self-supervised)	ResNet-34	Model seed (None, 0)
Information Alignment (IA)	Word-Speaker- Noise (supervised)	ResNet-18v2	Dataset seed (None, 0)
Feedback Alignment (FA)	CIFAR-10 (supervised)	ResNet-18	
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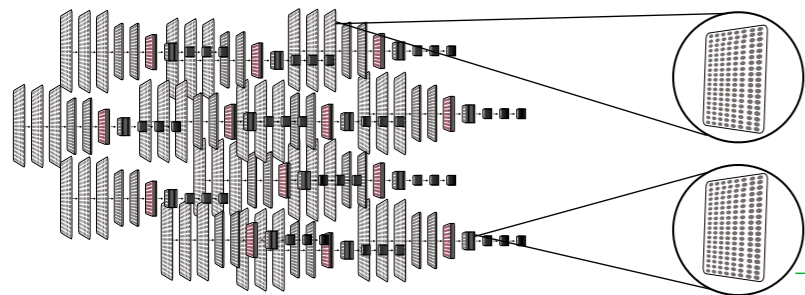


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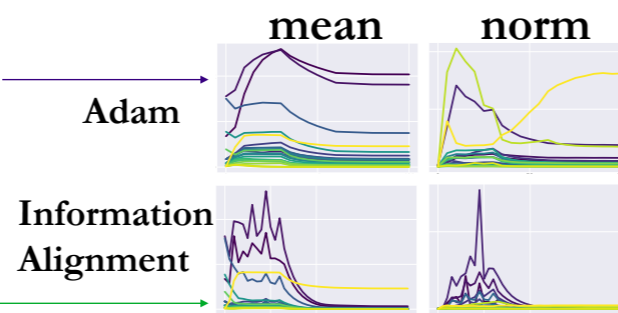
# “Virtual Experimental” Approach

## Data Generation



10 architectures, 4 tasks, 12  
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## Observable Statistics



Training  
Epochs

# Defining observable statistics

**Weights**

Proxy for synaptic strengths

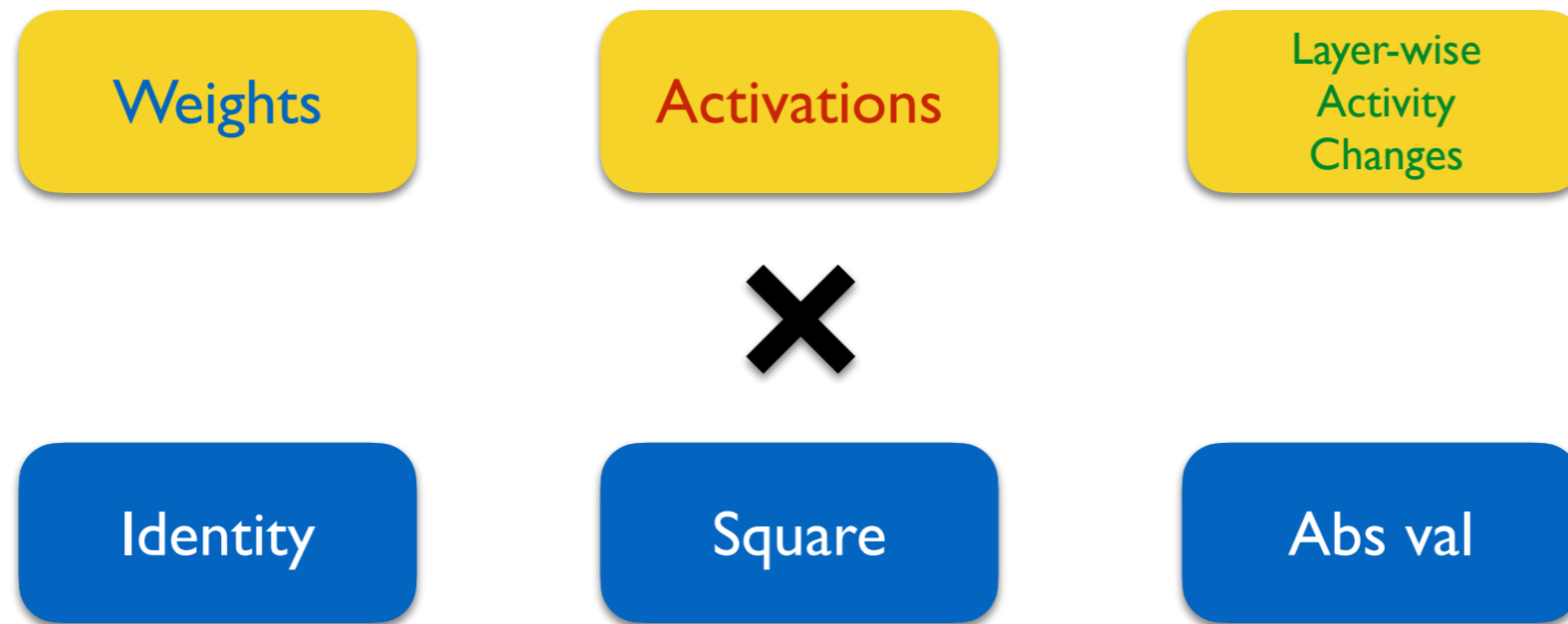
**Activations**

Proxy for post-synaptic activities

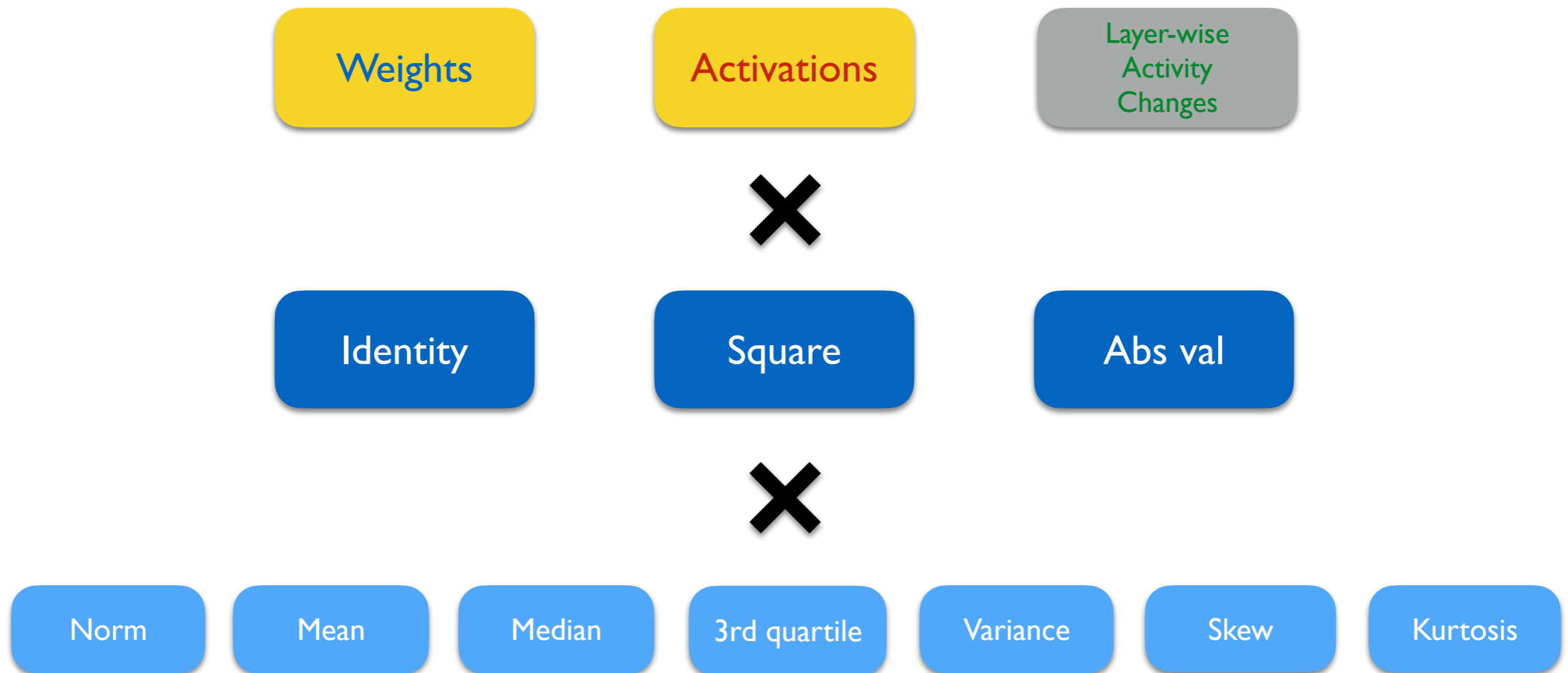
**Layer-wise  
Activity  
Changes**

Proxy for relative change between pre- and post-synaptic activations

# Defining observable statistics

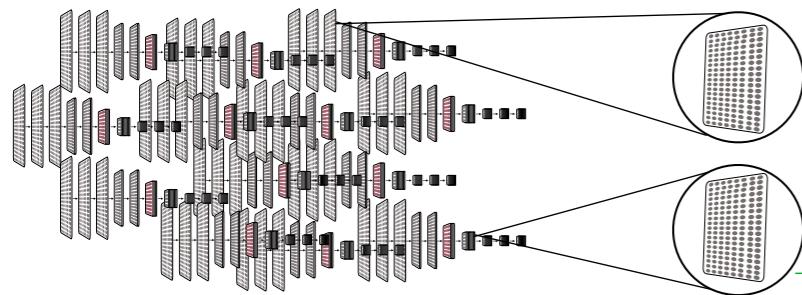


# Defining observable statistics



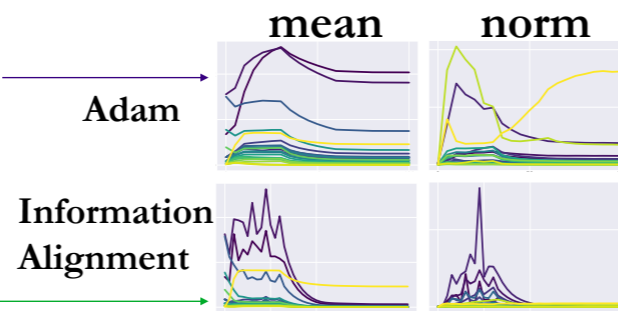
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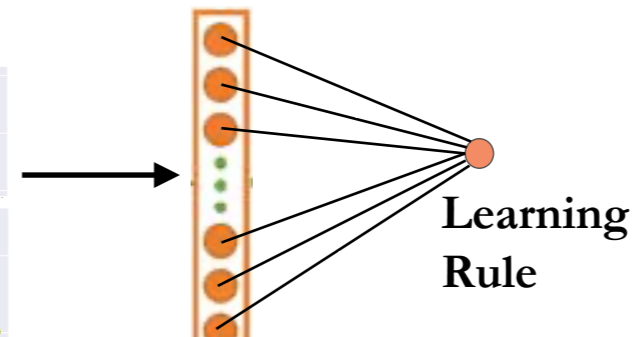
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## Observable Statistics



Training Epochs

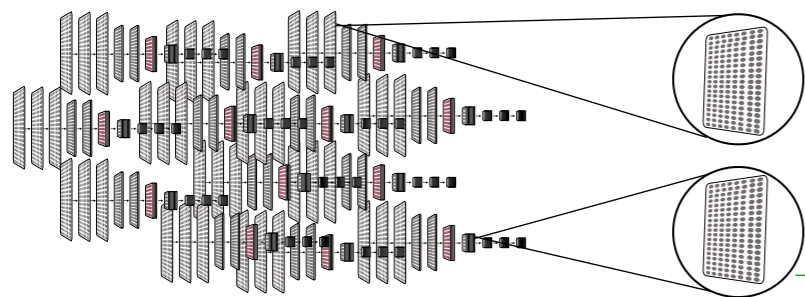
## Classifier Training



504  
Cross-validated,  
trained on split of  
observable trajectories

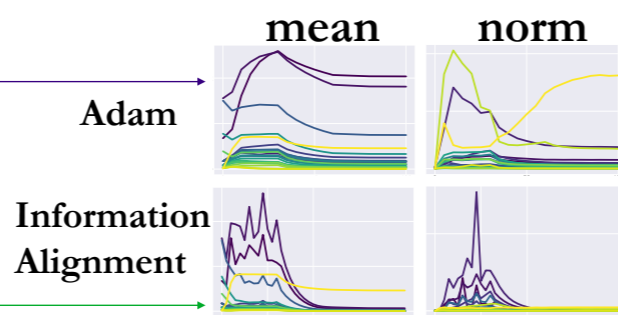
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## Data Generation



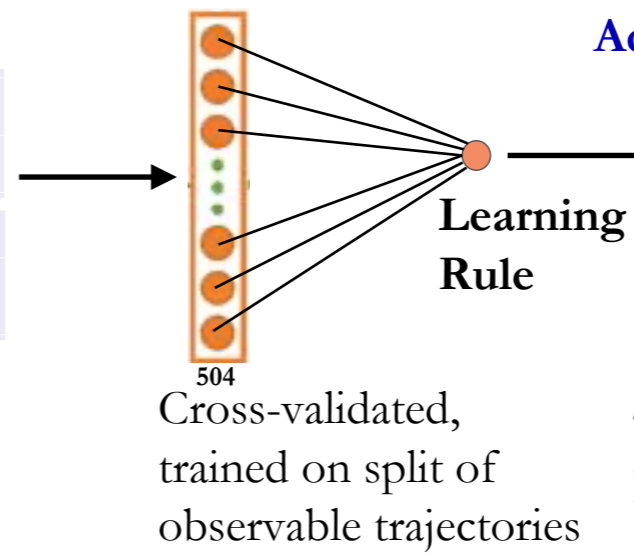
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## Observable Statistics



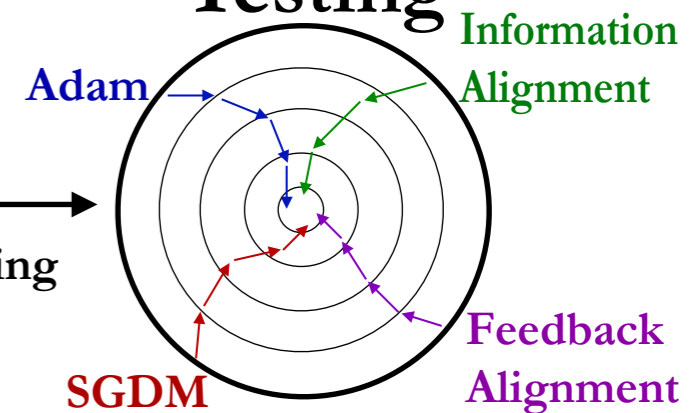
Training Epochs

## Classifier Training



504  
Cross-validated, trained on split of observable trajectories

## Classifier Testing



Tested on remaining data, held-out cases, etc.

Is this problem even tractable?

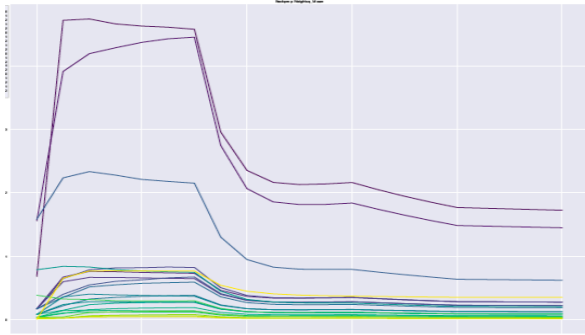


# Visualizing observables on ImageNet

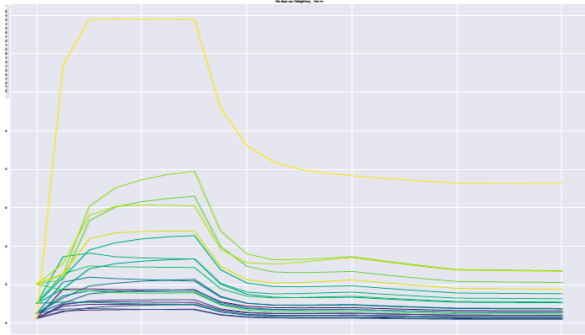
# Visualizing observables on ImageNet

SGDM

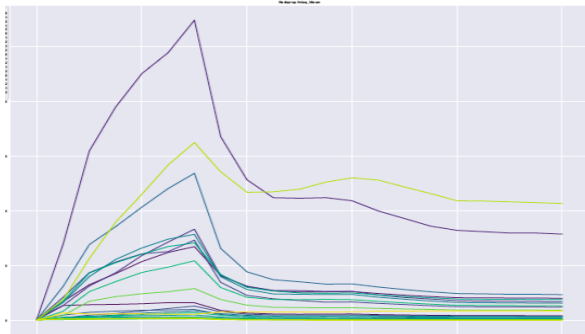
weight-square-mean



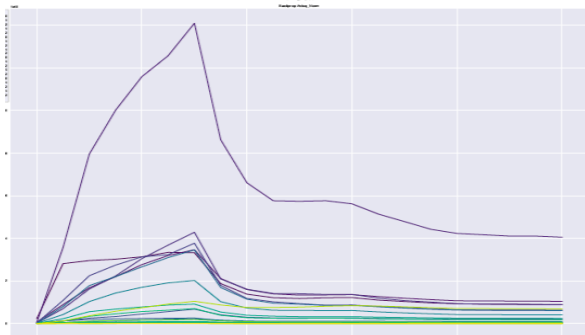
weight-square-norm



activation-square-mean

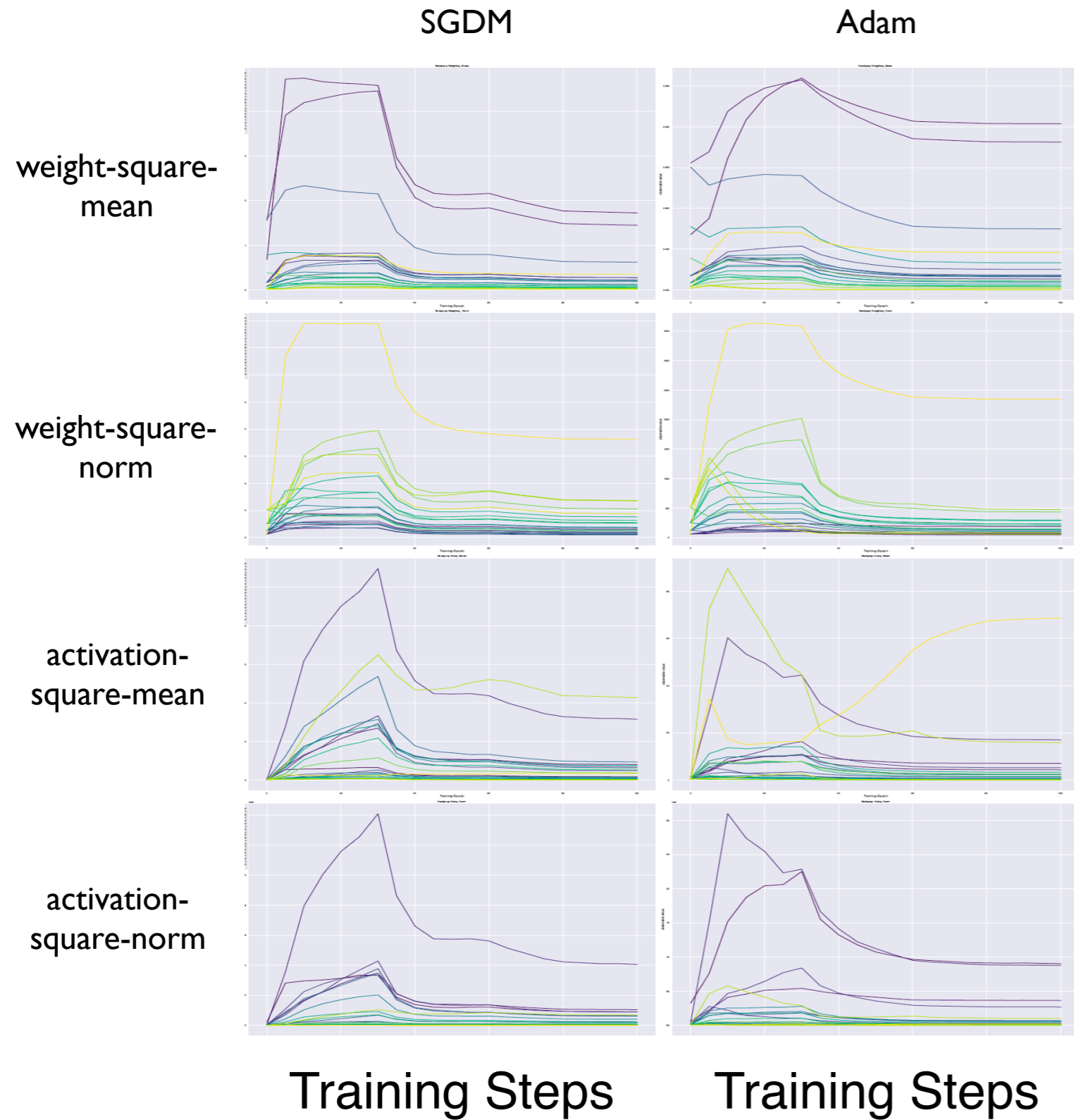


activation-square-norm

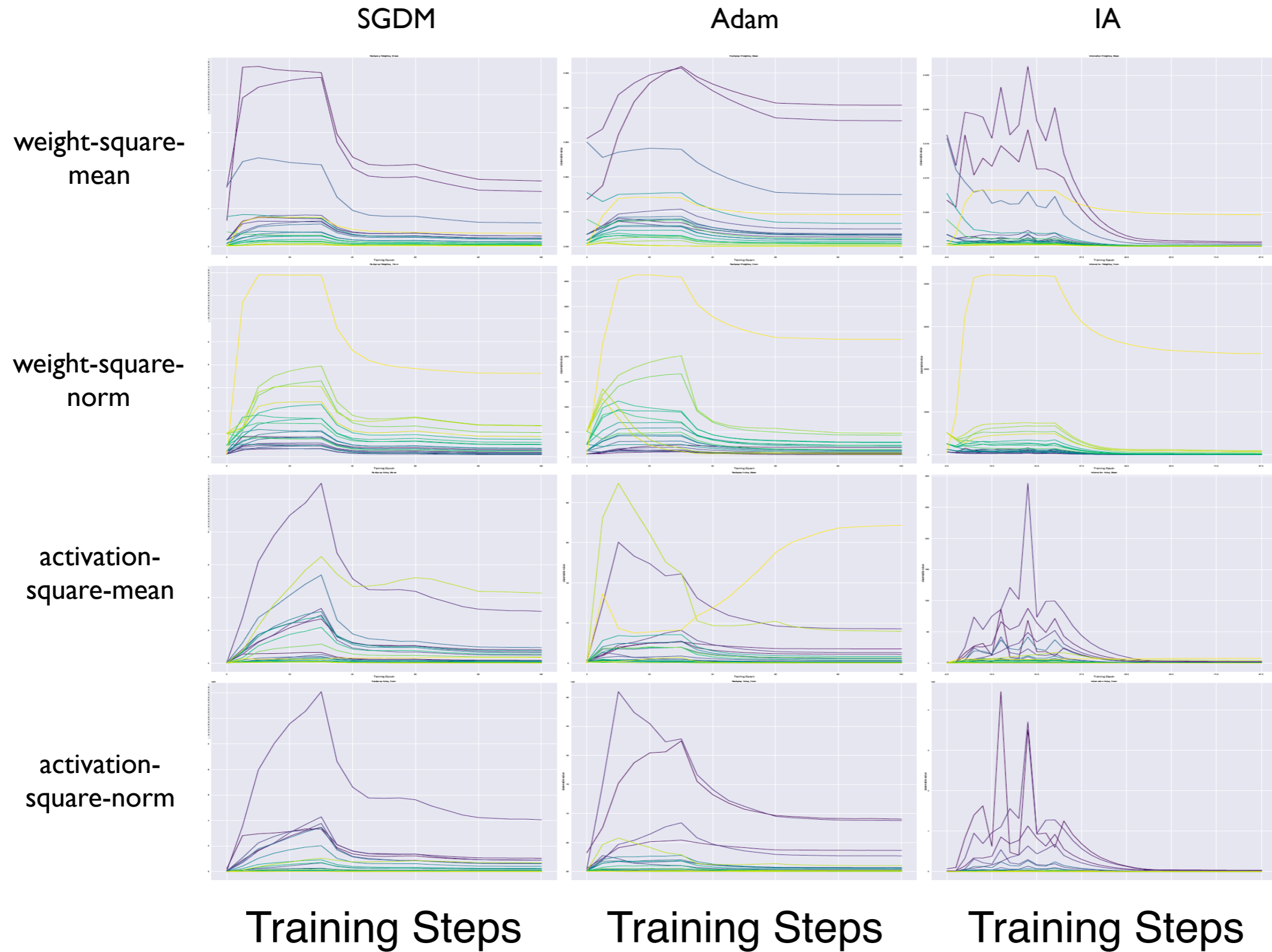


Training Steps

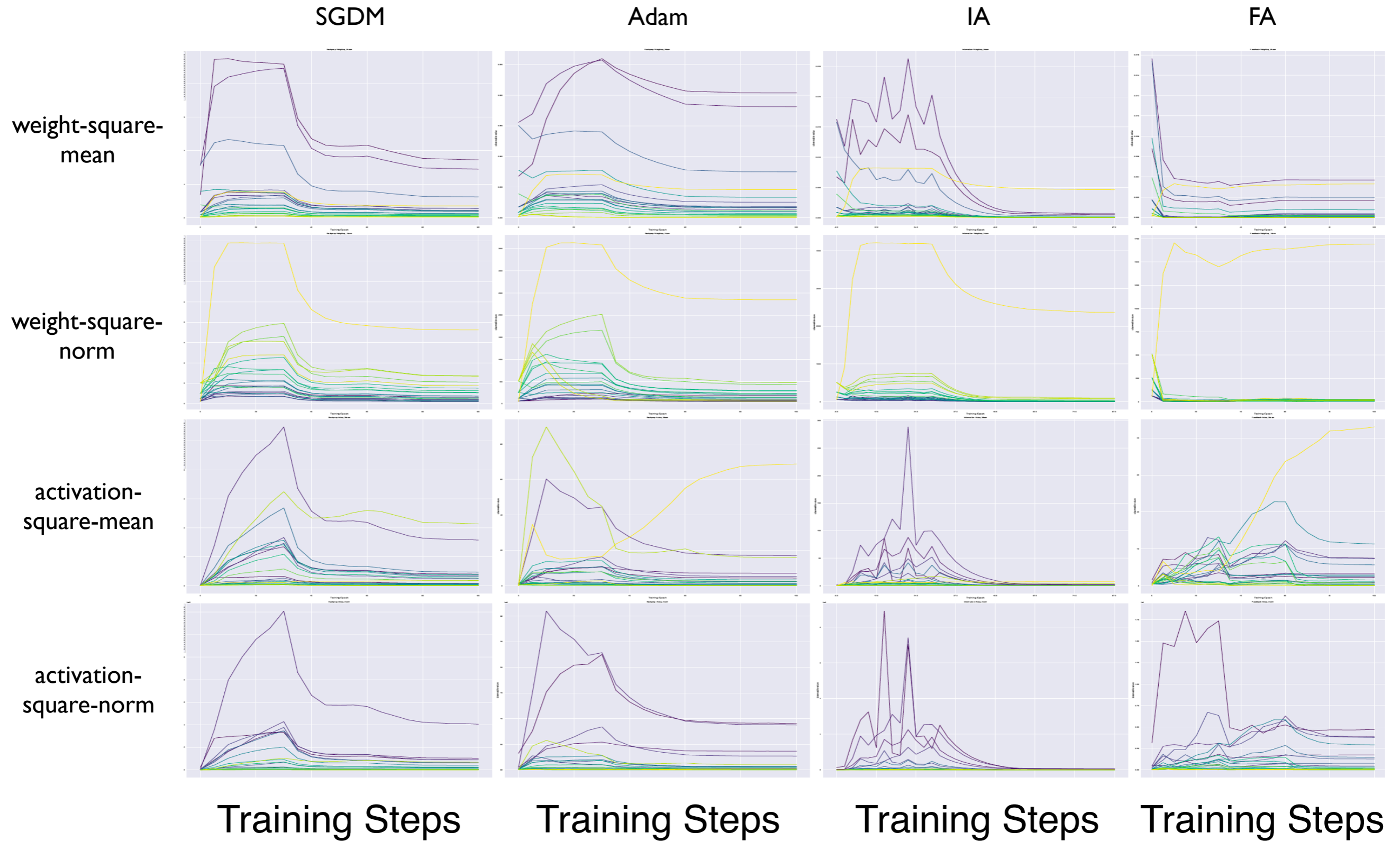
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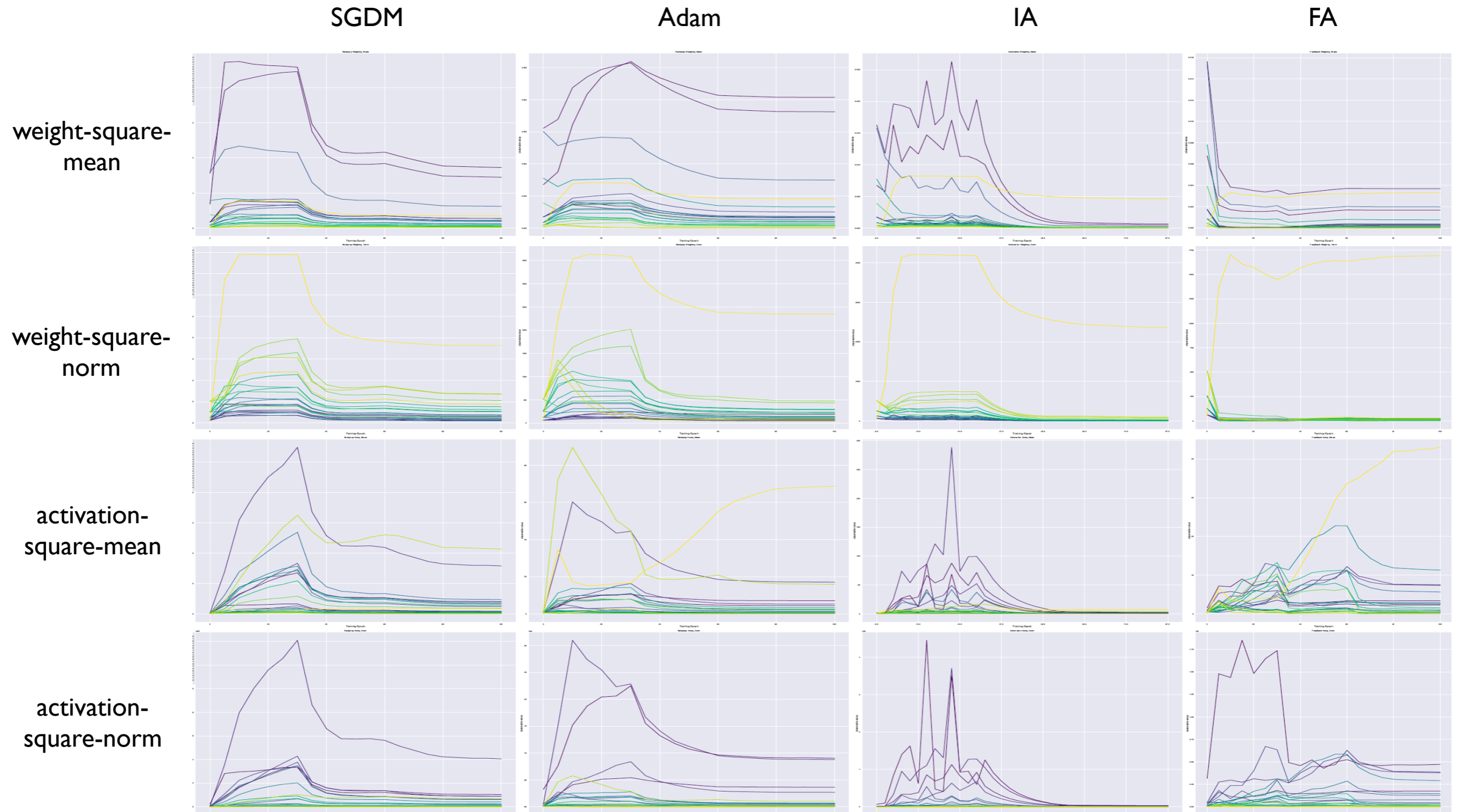
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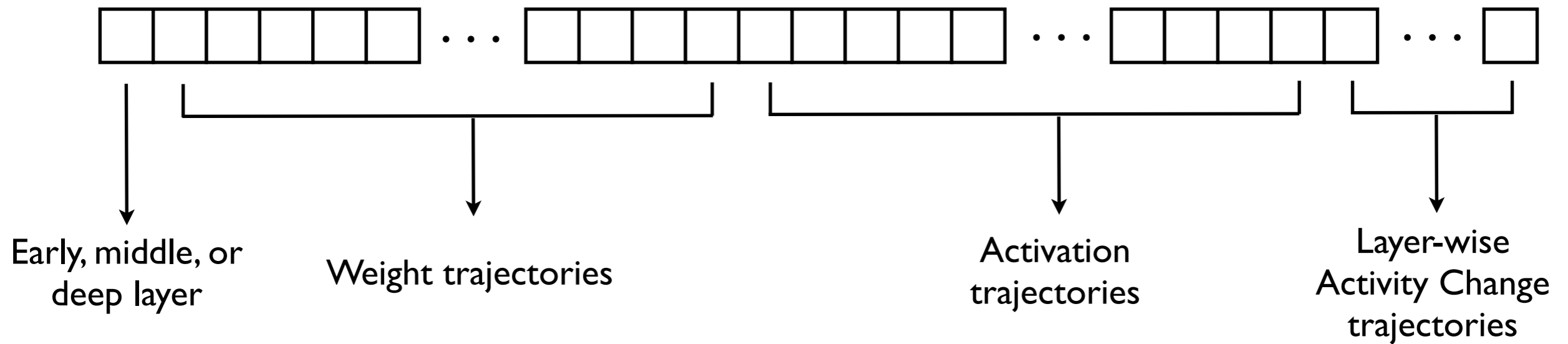


Trajectories across network training appear highly distinctive

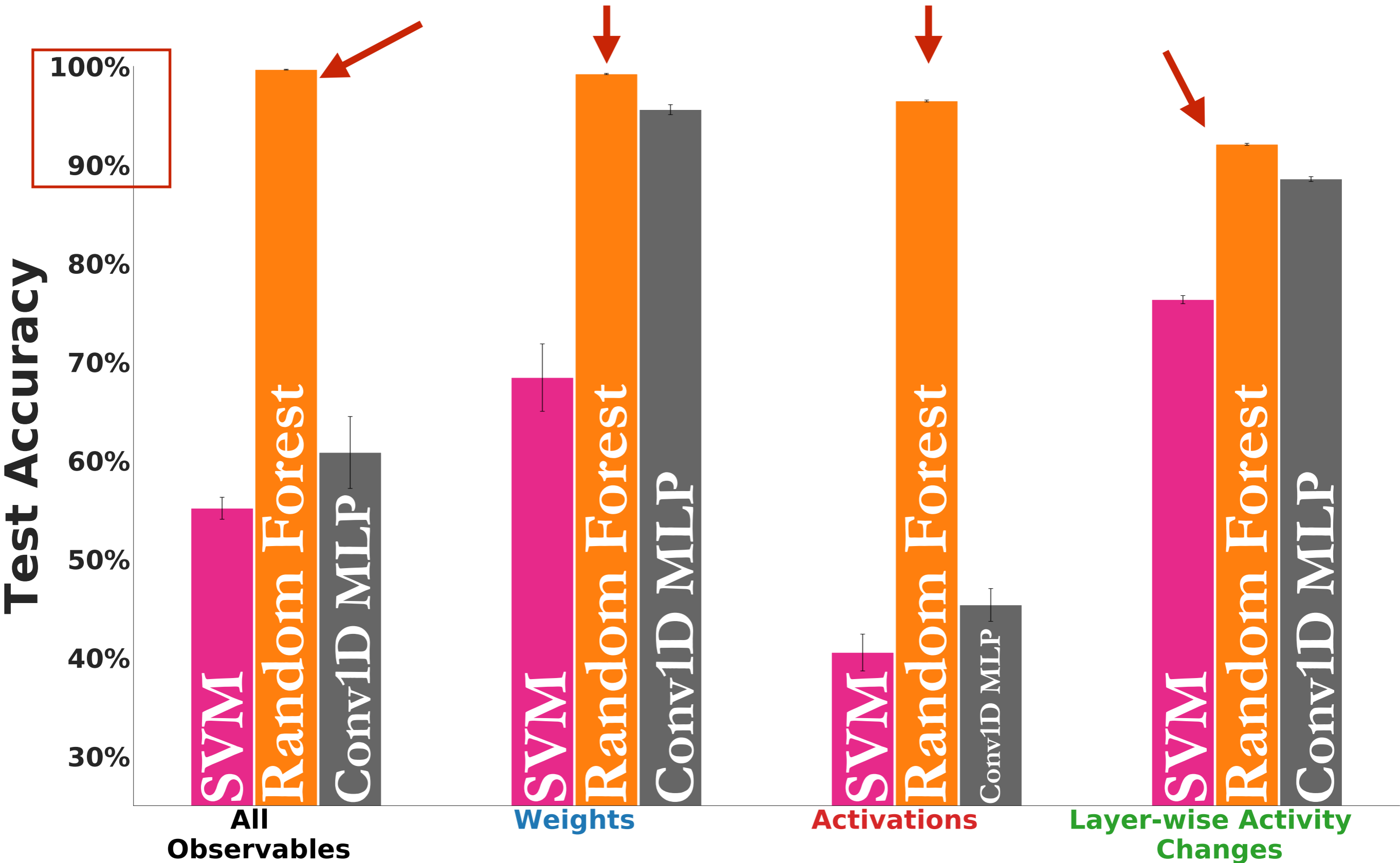
# Framing it as a classification problem

How well can we do by framing it as a classification problem?

Sample is constructed from one layer of a trained network

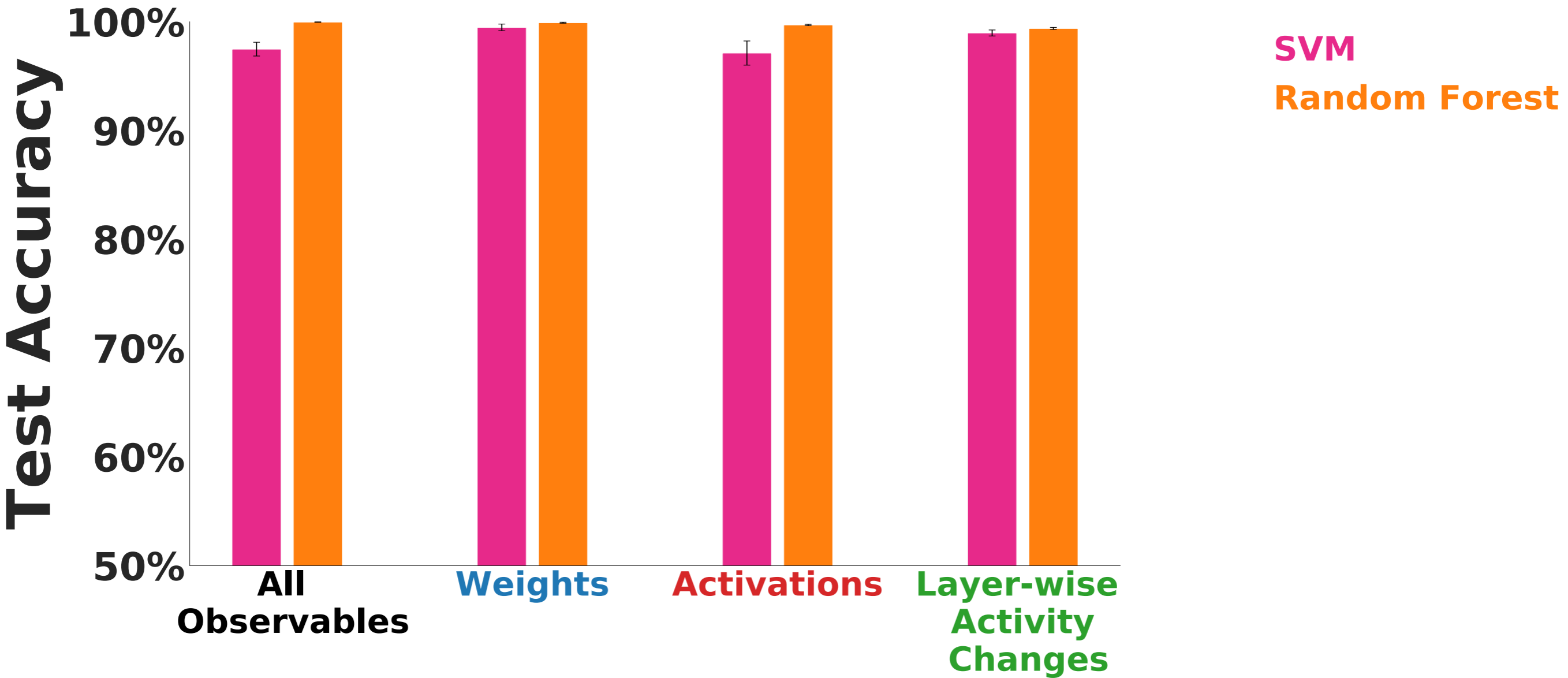


# General separability problem is tractable

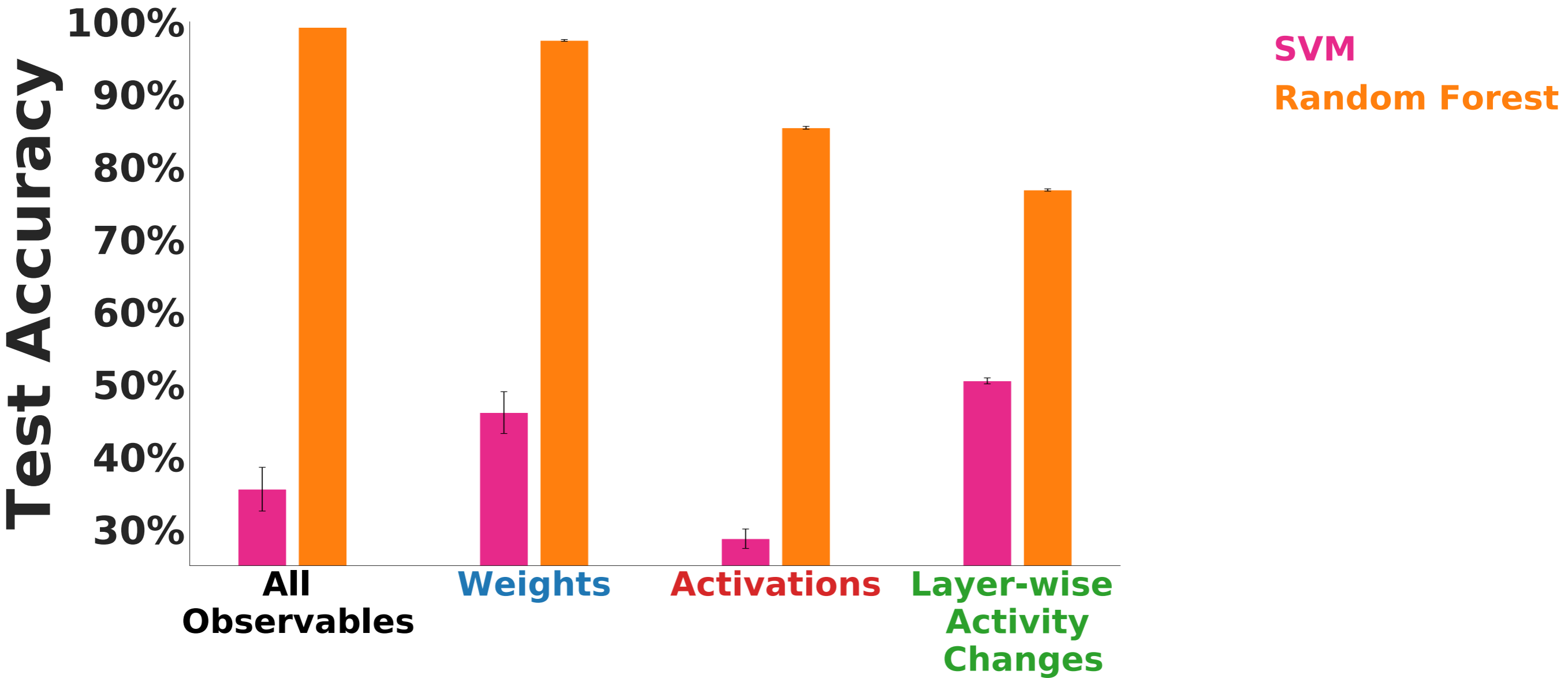




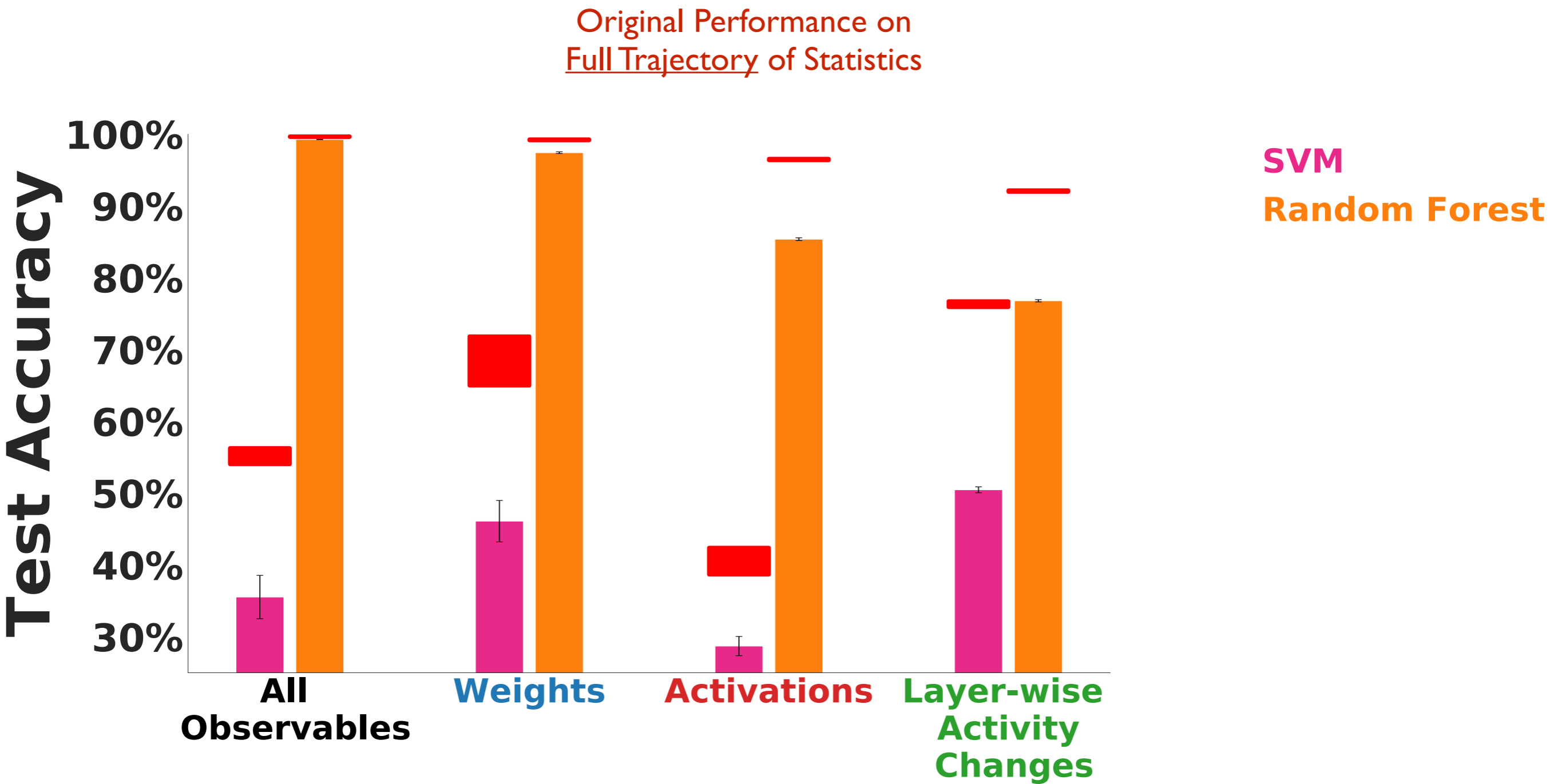
Not driven by task performance (where definable)



# Scale of observable statistics is *not* sufficient in most cases



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# Adding Experimental Realism

**Removing certain “animals” or “training curricula”:** holdouts of entire input classes

**Access to only portions of the learning trajectory:** subsampling observable trajectories

**Incomplete and noisy measurements:** subsampling units and Gaussian noise before collecting observables

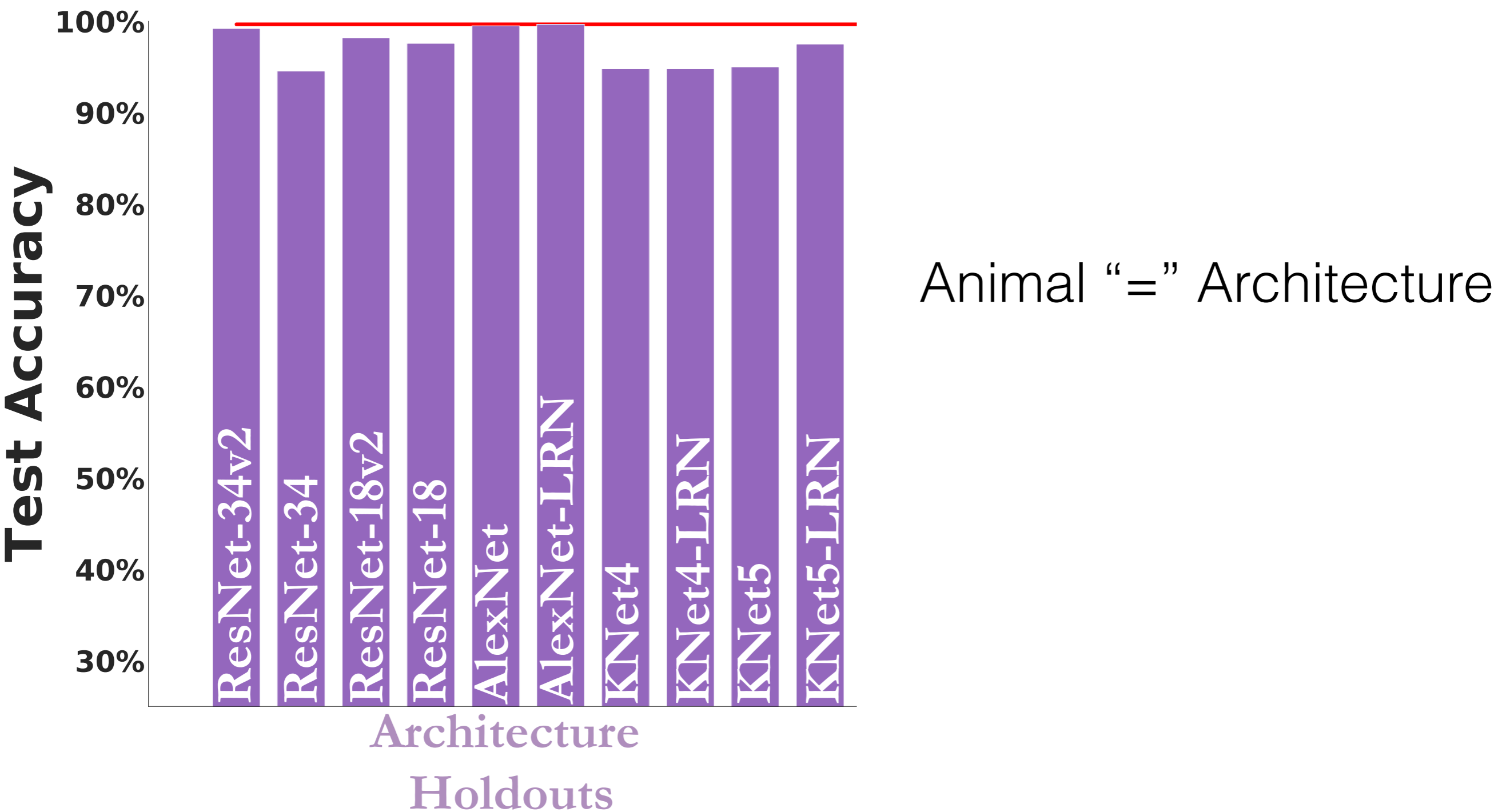
# Adding Experimental Realism

**Removing certain “animals” or “training curricula”:** holdouts of entire input classes

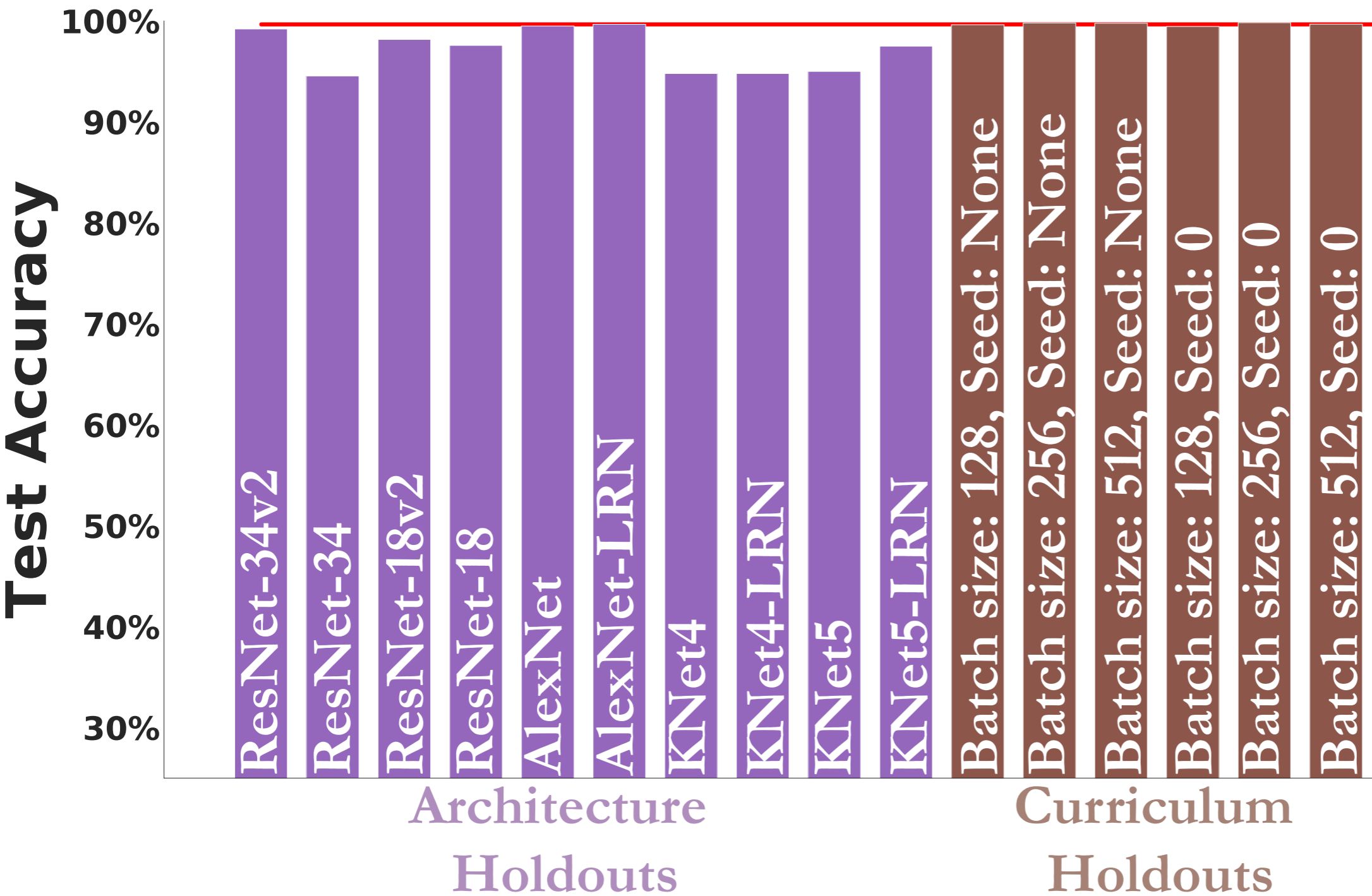
**Access to only portions of the learning trajectory:** subsampling observable trajectories

**Incomplete and noisy measurements:** subsampling units and Gaussian noise before collecting observables

# Generalization to held-out “animals”



# Generalization to held-out “training curricula”



# Adding Experimental Realism

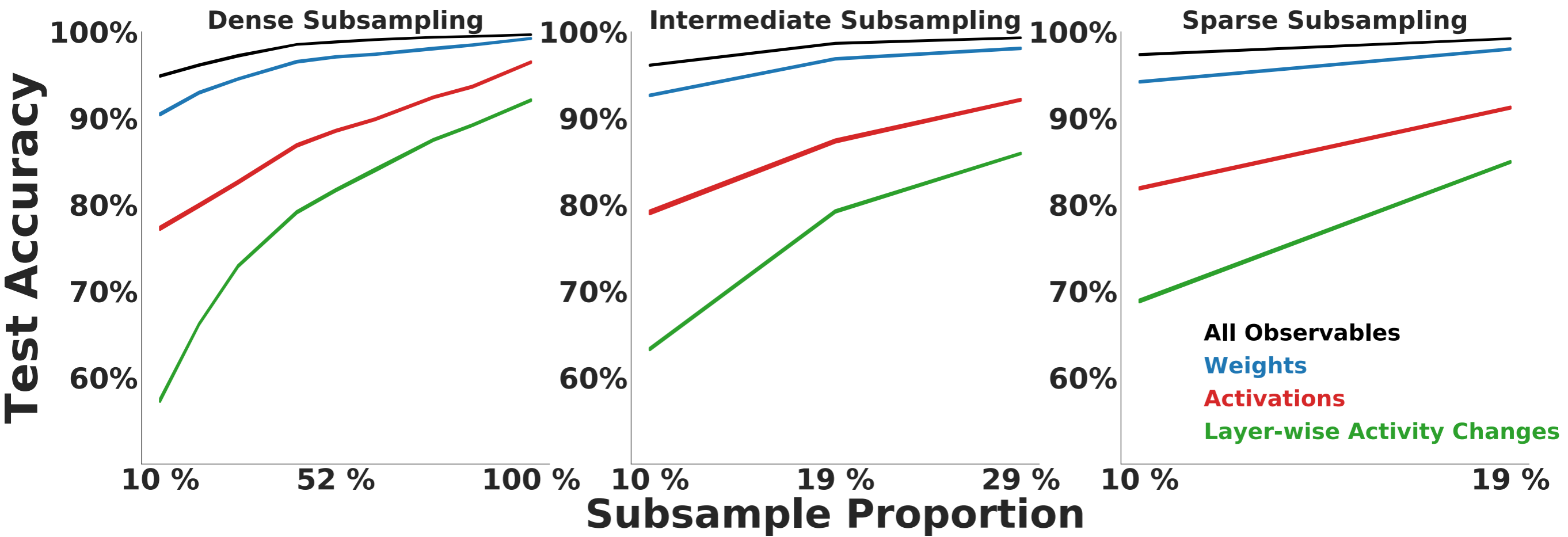
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# Sparse subsampling across learning trajectory robust to trajectory undersampling



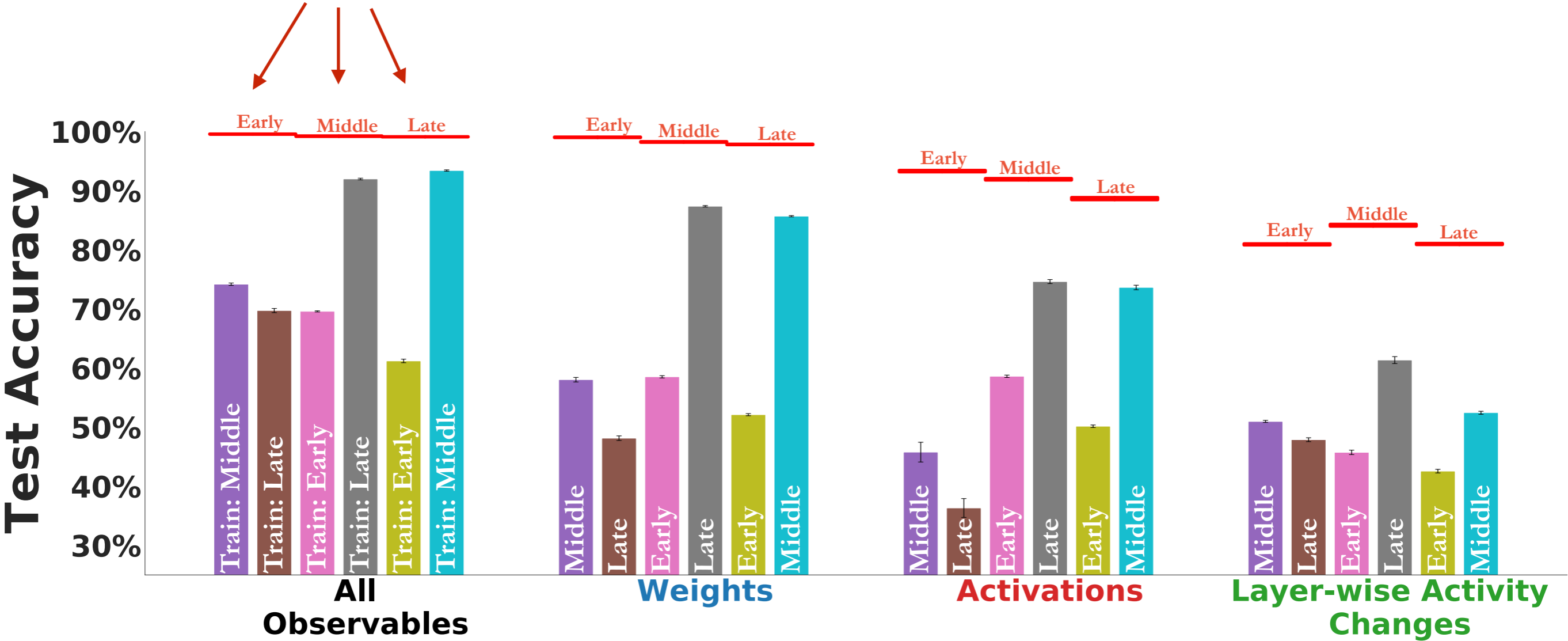
Least Robust



Most Robust

# Sampling across learning trajectory is important for robustness to undersampling

Original performance  
on held-out portions



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What insights could this approach potentially provide?

## **Different experimental tools have different limitations**

Optical imaging techniques usually give us simultaneous access to thousands of units but can have lower temporal resolution and signal-to-noise

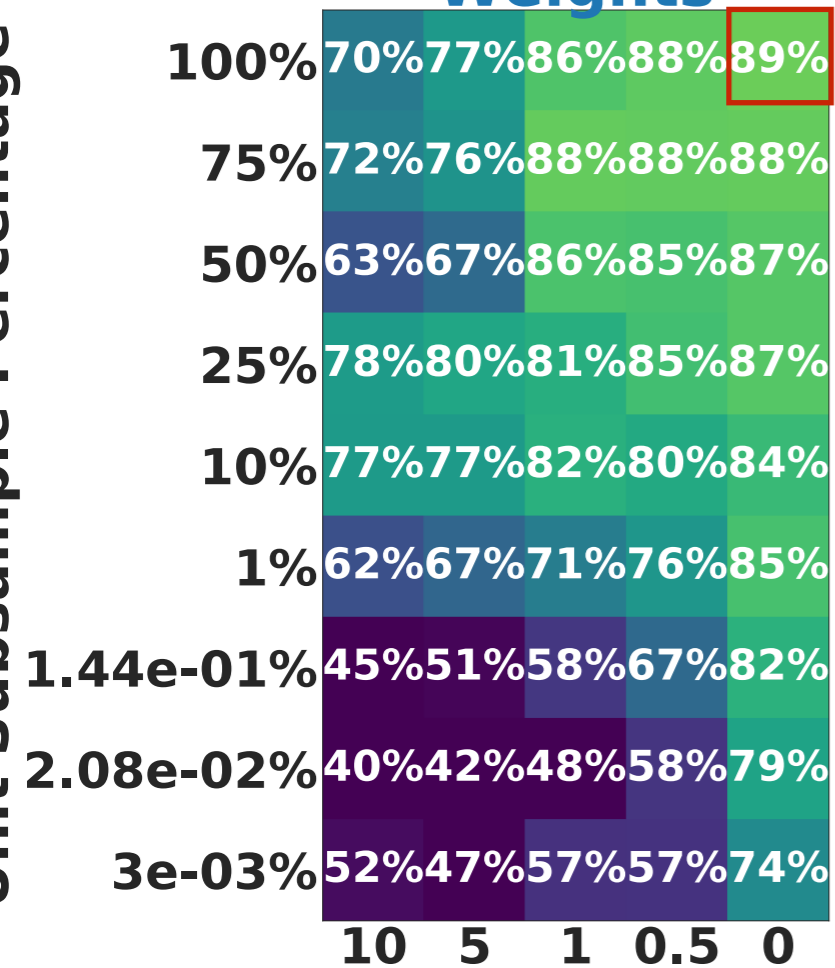
Electrophysiological recordings can have higher signal-to-noise and better temporal resolution, but can lack the coverage to thousands of units

# Modeling unit subsampling and measurement noise

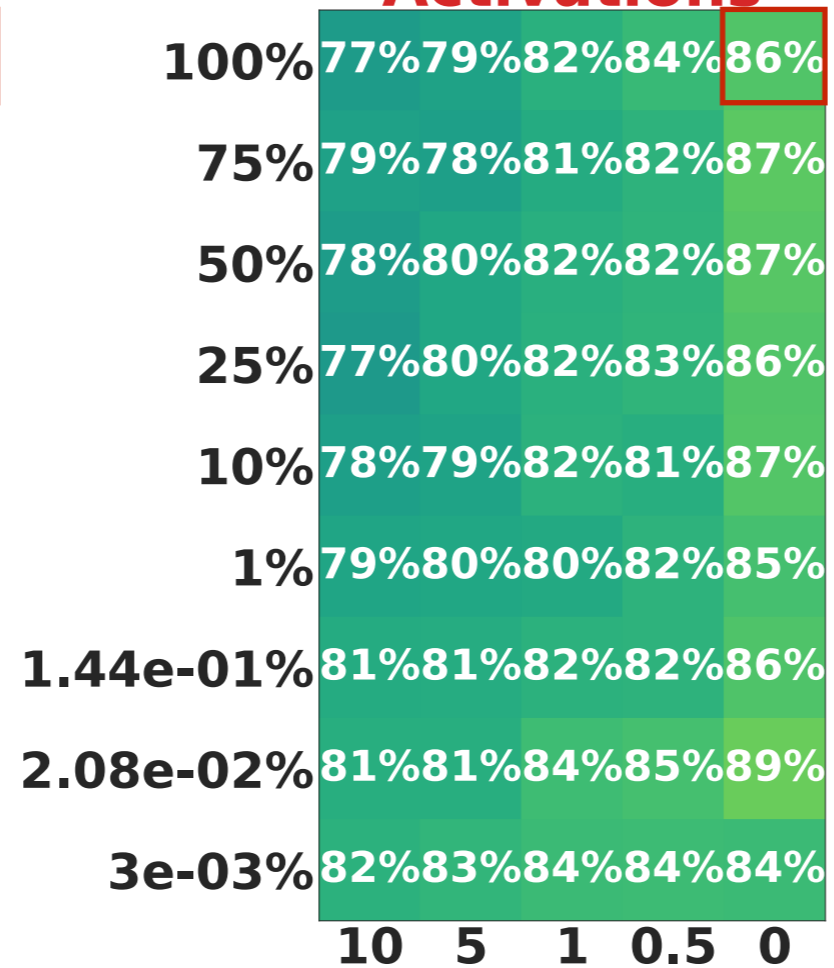
“Ideal” noiseless, perfect information setting

Unit Subsample Percentage

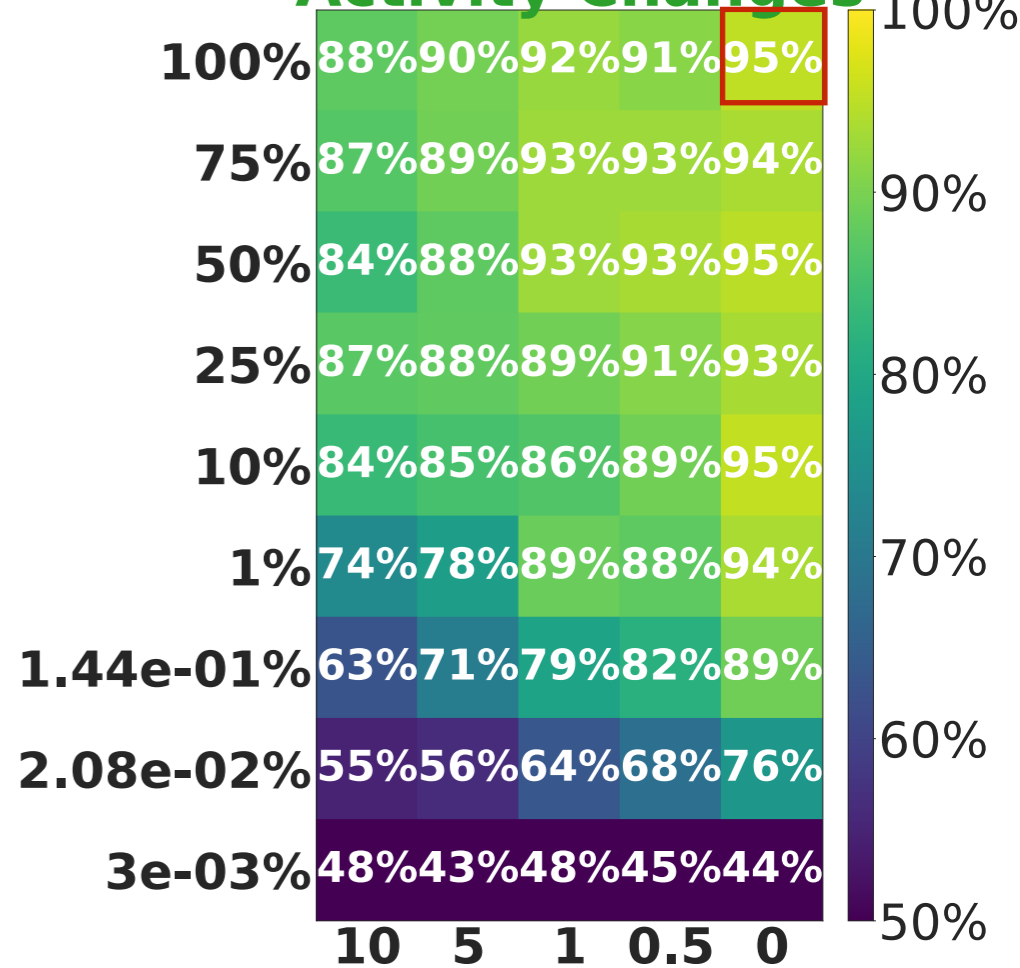
Weights



Activations



Layer-wise Activity Changes



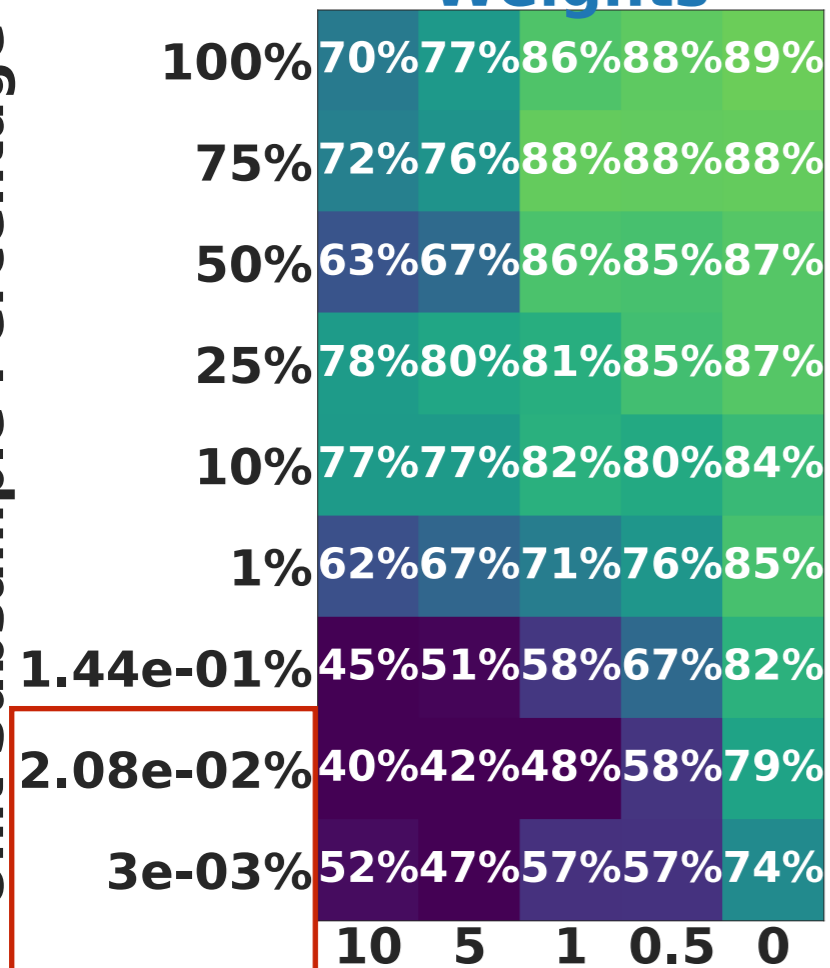
Gaussian Noise  $\sigma$

# Weights are *not* robust to measurement noise and unit undersampling

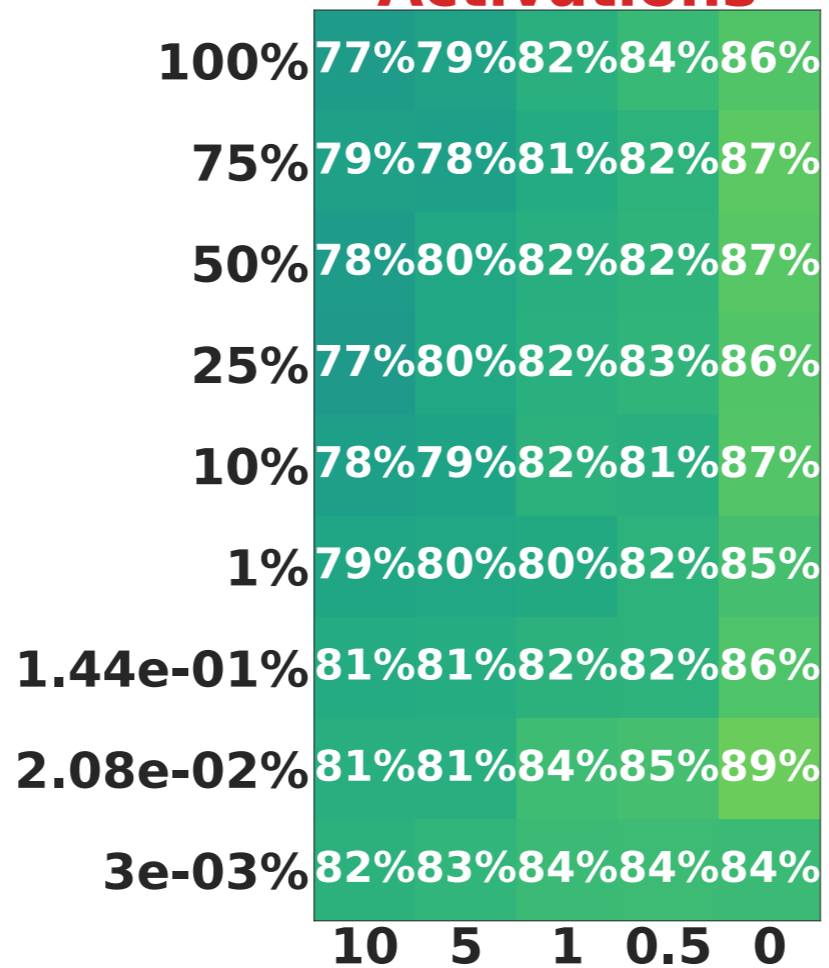


Unit Subsample Percentage

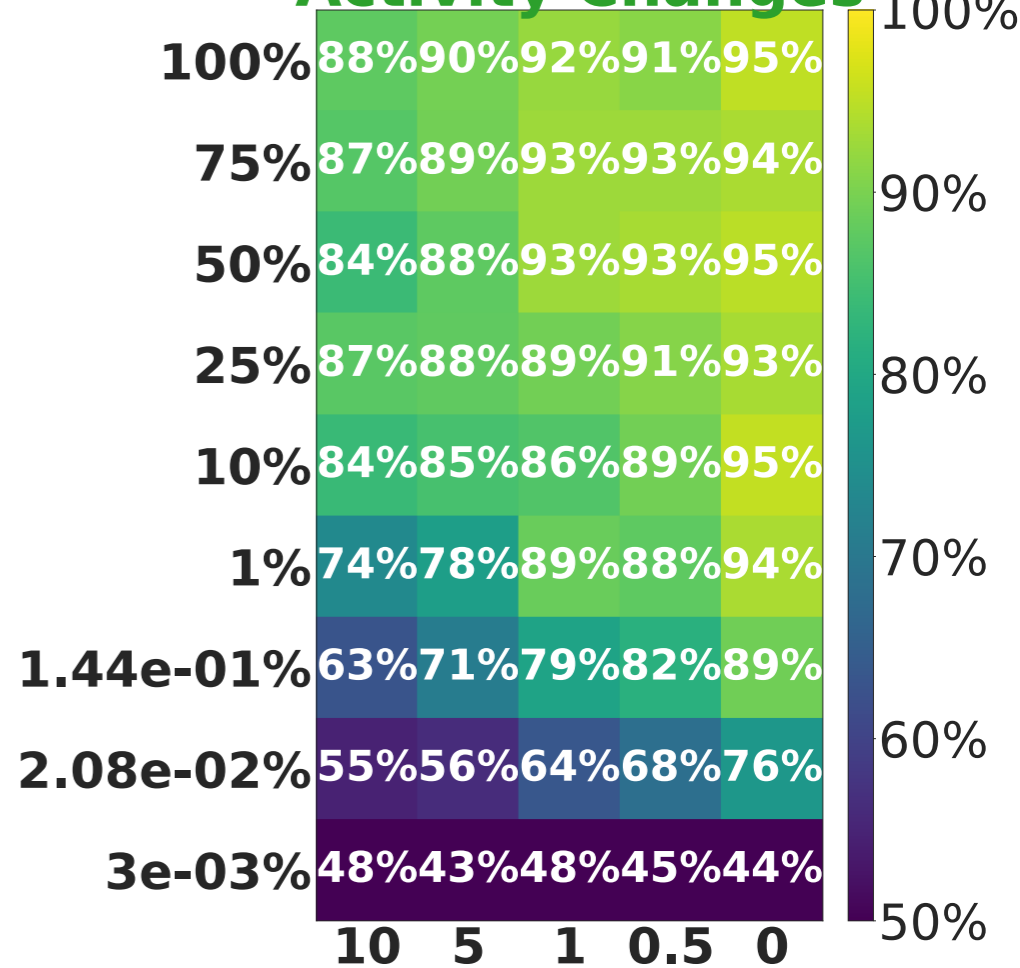
### Weights



### Activations



### Layer-wise Activity Changes

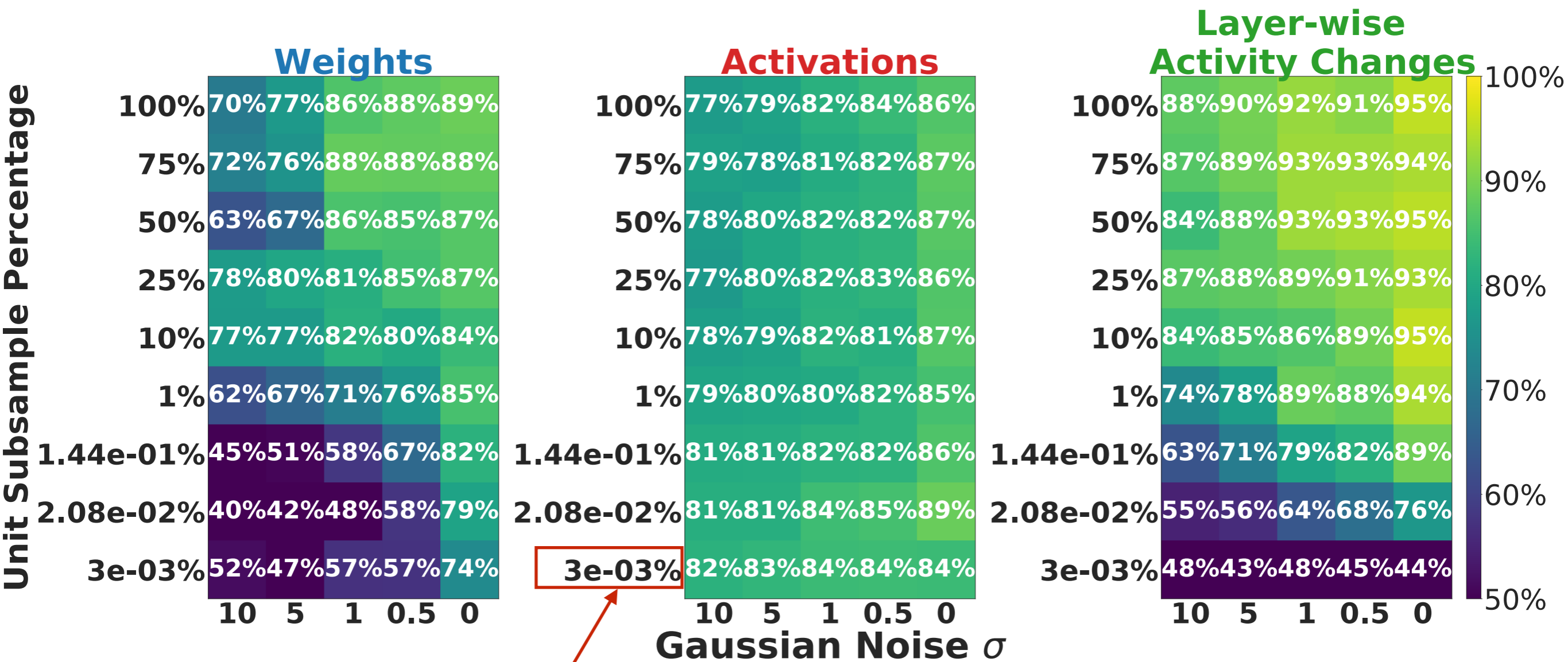


Gaussian Noise  $\sigma$



Within typical imaging range of several hundred to several thousand synapses

Activations are the most robust to measurement noise and unit undersampling



Within typical electrophysiological range of several hundred units 

# Conclusions



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We can identify learning rules *only* on the basis of aggregate statistics of observable measures: weights, activations, or layer-wise activity changes

# Conclusions

**Hypothesis:** *in vivo* electrophysiological recordings of post-synaptic activities from a neural circuit on the order of several hundred units, frequently measured at wider intervals during the course of learning, may provide a good basis on which to identify learning rules

We can identify learning rules *only* on the basis of aggregate statistics of observable measures: weights, activations, or layer-wise activity changes

This observation holds across various scenarios of experimental realism of certain held-out input classes, trajectory undersampling, and unit undersampling & measurement noise, with network activations being the most robust

# Acknowledgements

Thanks!

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Surya Ganguli



Daniel Yamins



**NeurIPS 2020 Paper:** <https://arxiv.org/abs/2010.11765>

**Code & Dataset:** <https://github.com/neuroailab/lr-identify>

**Experimental collaborations welcome!**